CS4212: Compiler Design

- Week 13:
- General Dataflow Analysis Framework **Register** Allocation
 - Wrap-Up

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Previous Lectures: Liveness

- lacksquare
- Liveness is defined in terms of where variables are *defined* and where variables are *used*
- Liveness analysis: Compute the live variables between each statement. \bullet
 - _____
 - To be useful, it should be more *precise* than simple scoping rules. ____

A variable v is *live* at a program point if v is defined before the program point and used after it.

May be conservative (i.e. it may claim a variable is live when it isn't) so because that's a safe approximation



Simple Liveness Analysis Algorithm

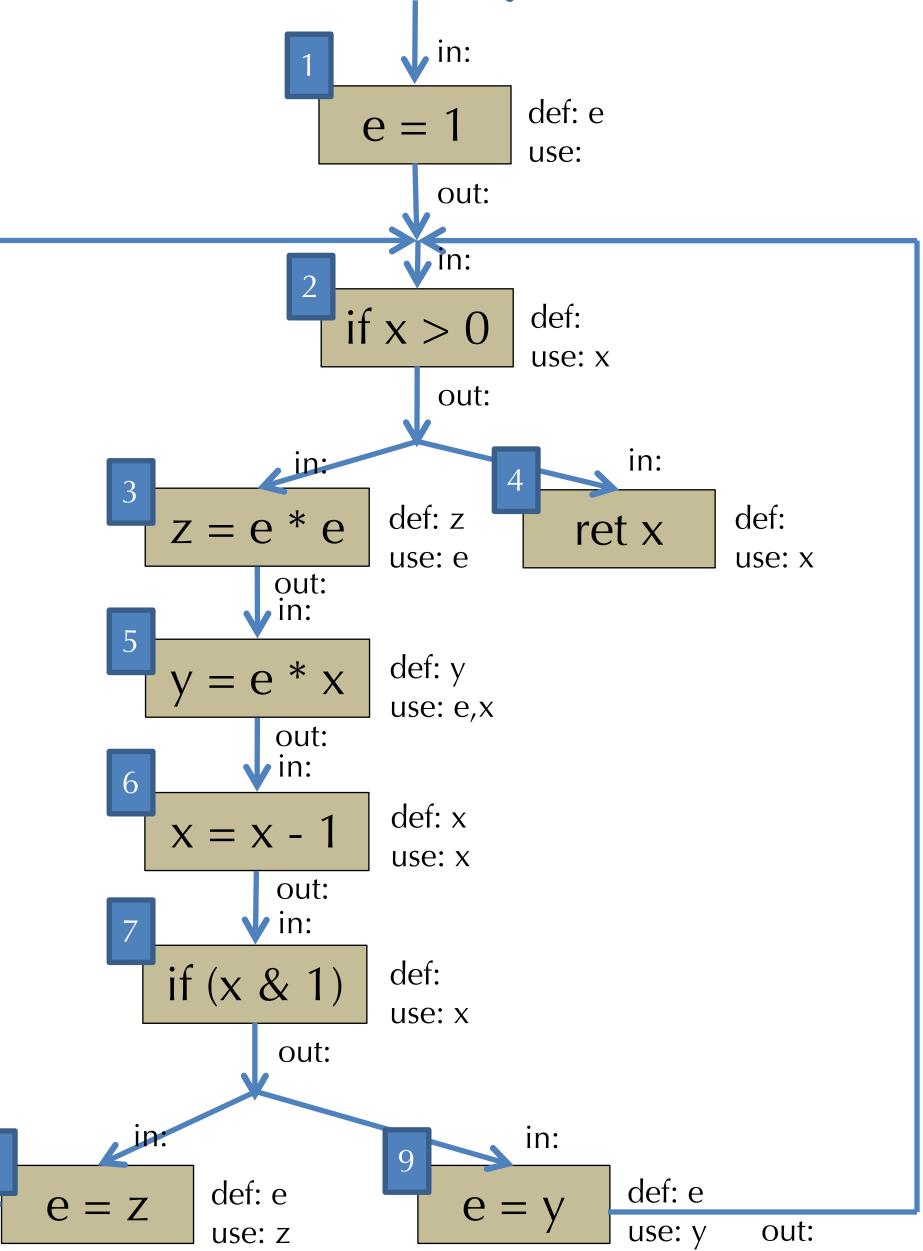
for all n, $in[n] := \emptyset$, $out[n] := \emptyset$ repeat until no change in 'in' and 'out' for all n out[n] := $\bigcup_{n' \in succ[n]} in[n']$ end end

Finds a *fixpoint* of the in and out equations. •

- $in[n] := use[n] \cup (out[n] def[n])$

Example Liveness Analysis

• Example flow graph:

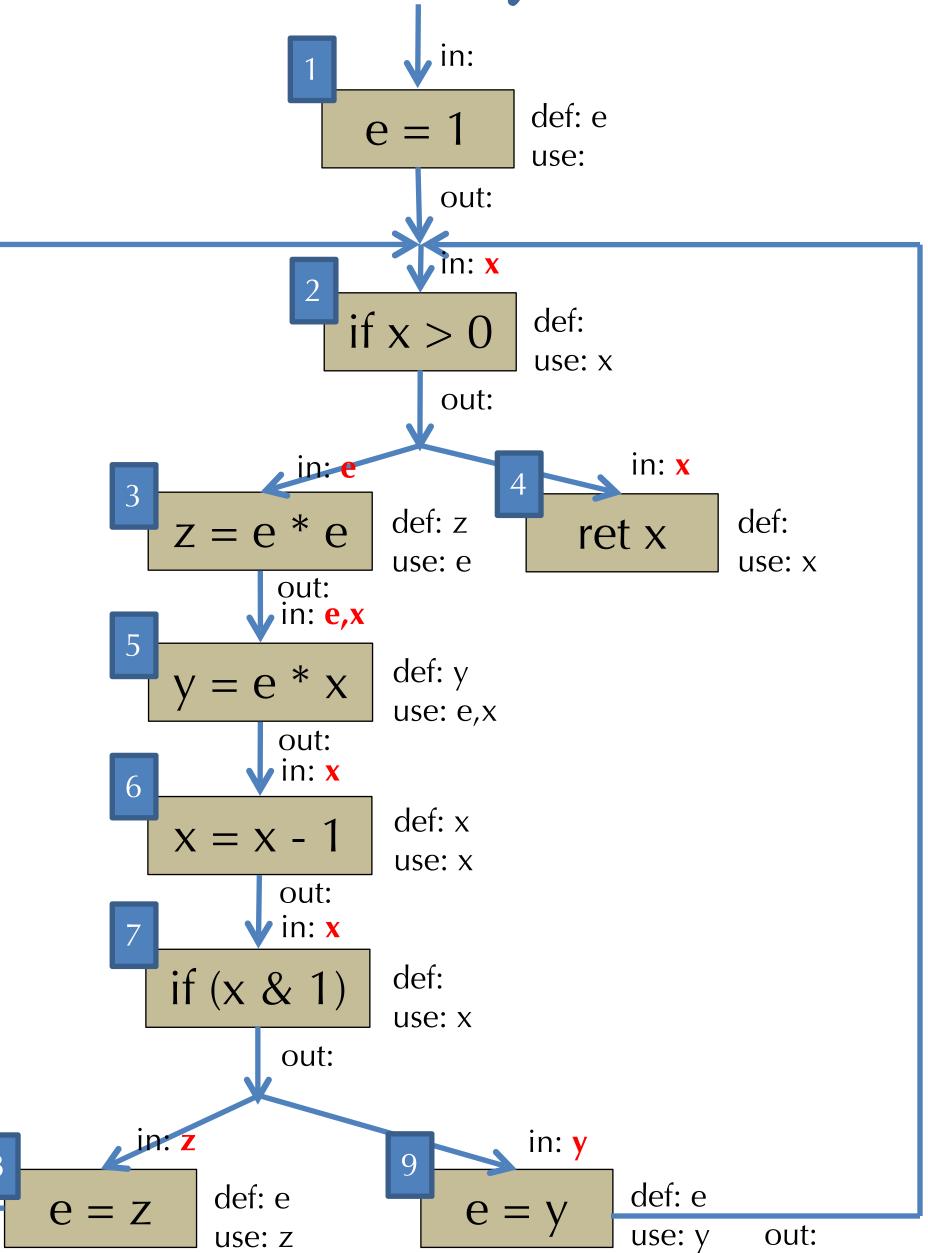


Example Liveness Analysis

Each iteration update: $out[n] := \bigcup_{n' \in succ[n]} in[n']$ $in[n] := use[n] \cup (out[n] - def[n])$

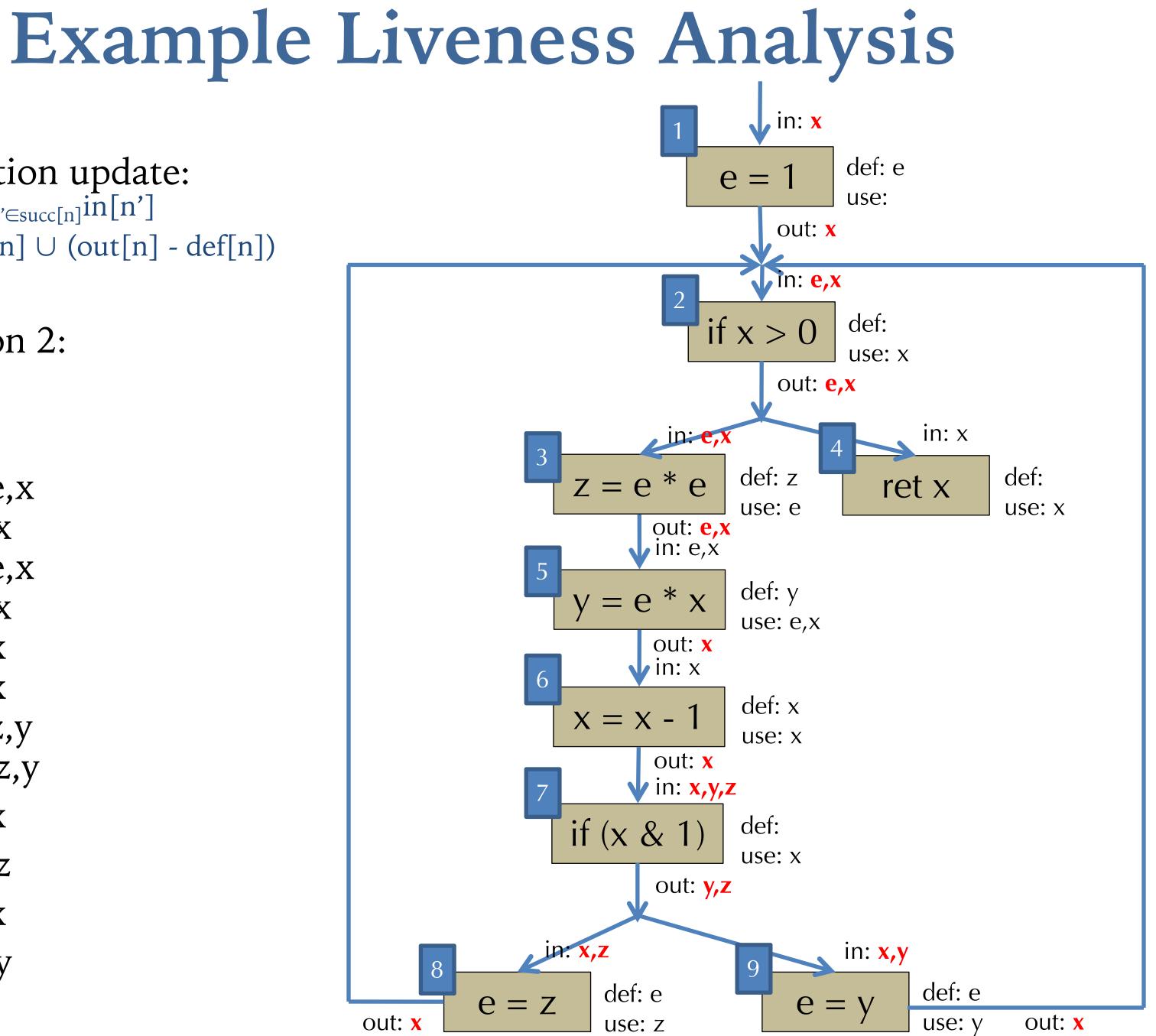
Iteration 1:
in[2] = x
in[3] = e
in[4] = x
in[5] = e,x
in[6] = x
in[7] = x
in[7] = z
in[9] = y

(showing only updates that make a change)

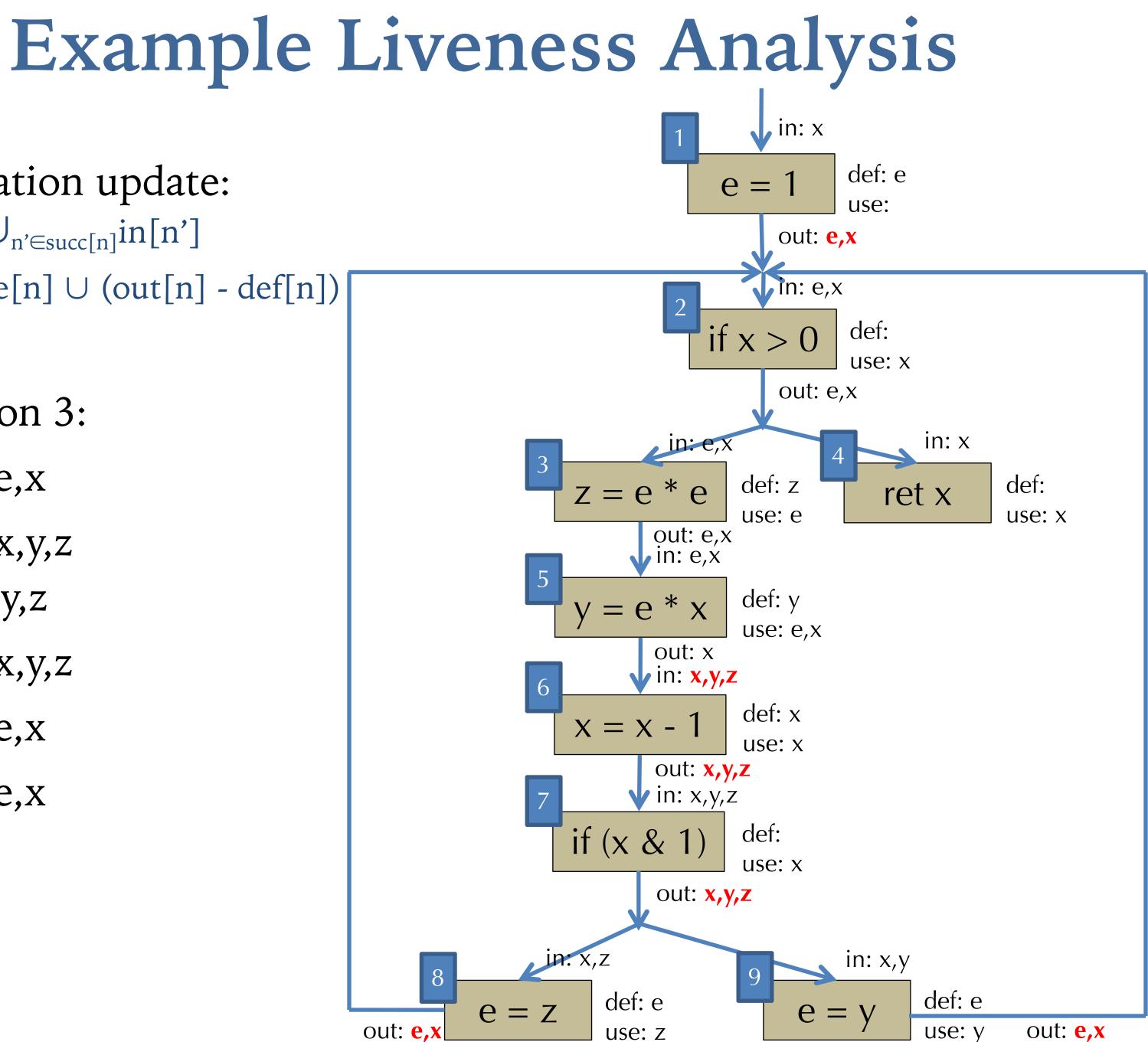


Iteration 2: ulletout[1] = xin[1] = xout[2] = e,xin[2] = e,xout[3] = e,xin[3] = e,xout[5] = xout[6] = xout[7] = z,yin[7] = x, z, yout[8] = xin[8] = x, zout[9] = xin[9] = x,y

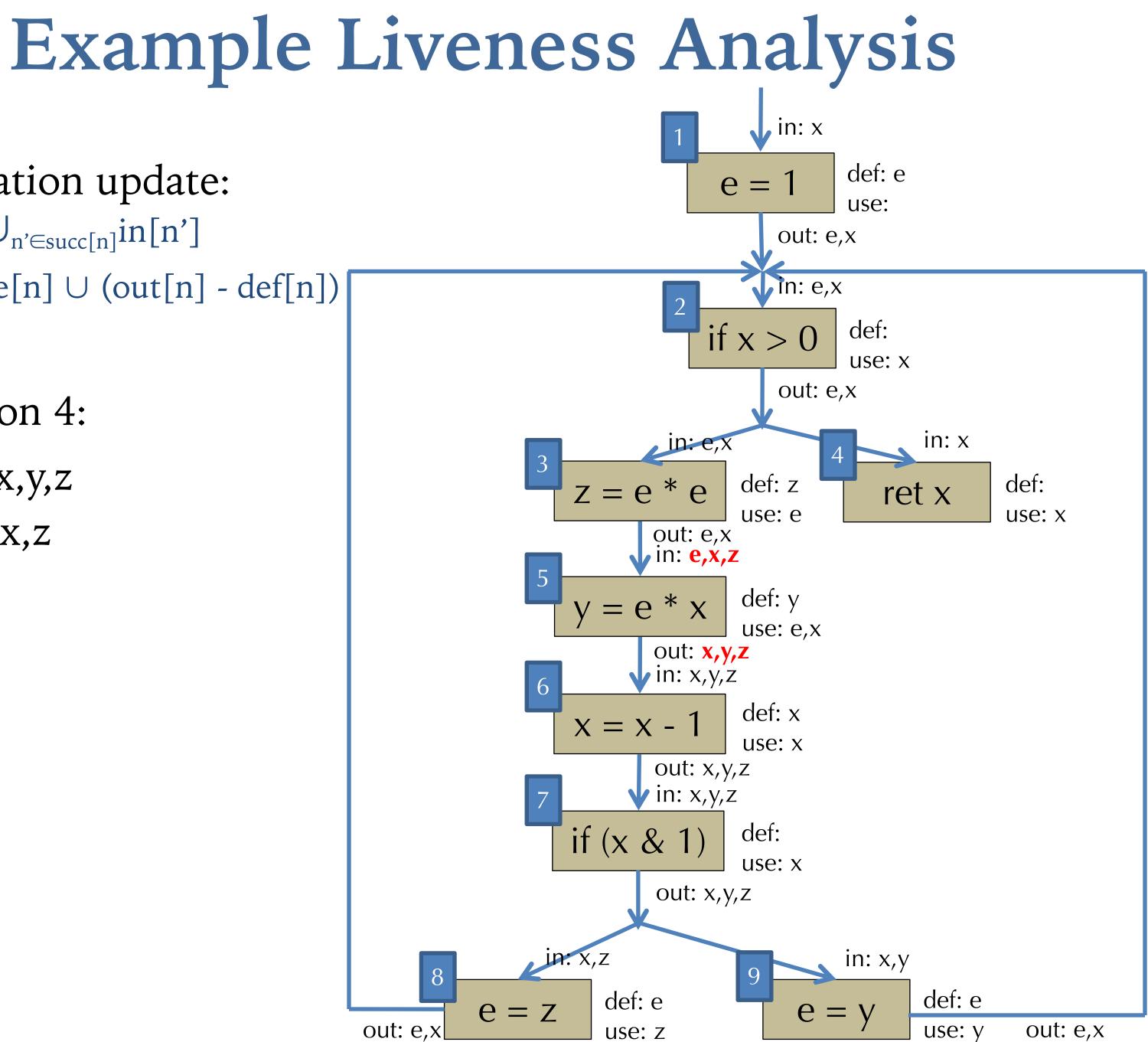
out: X



Iteration 3: ulletout[1] = e,xout[6] = x,y,zin[6] = x,y,zout[7] = x,y,zout[8] = e,xout[9] = e,x



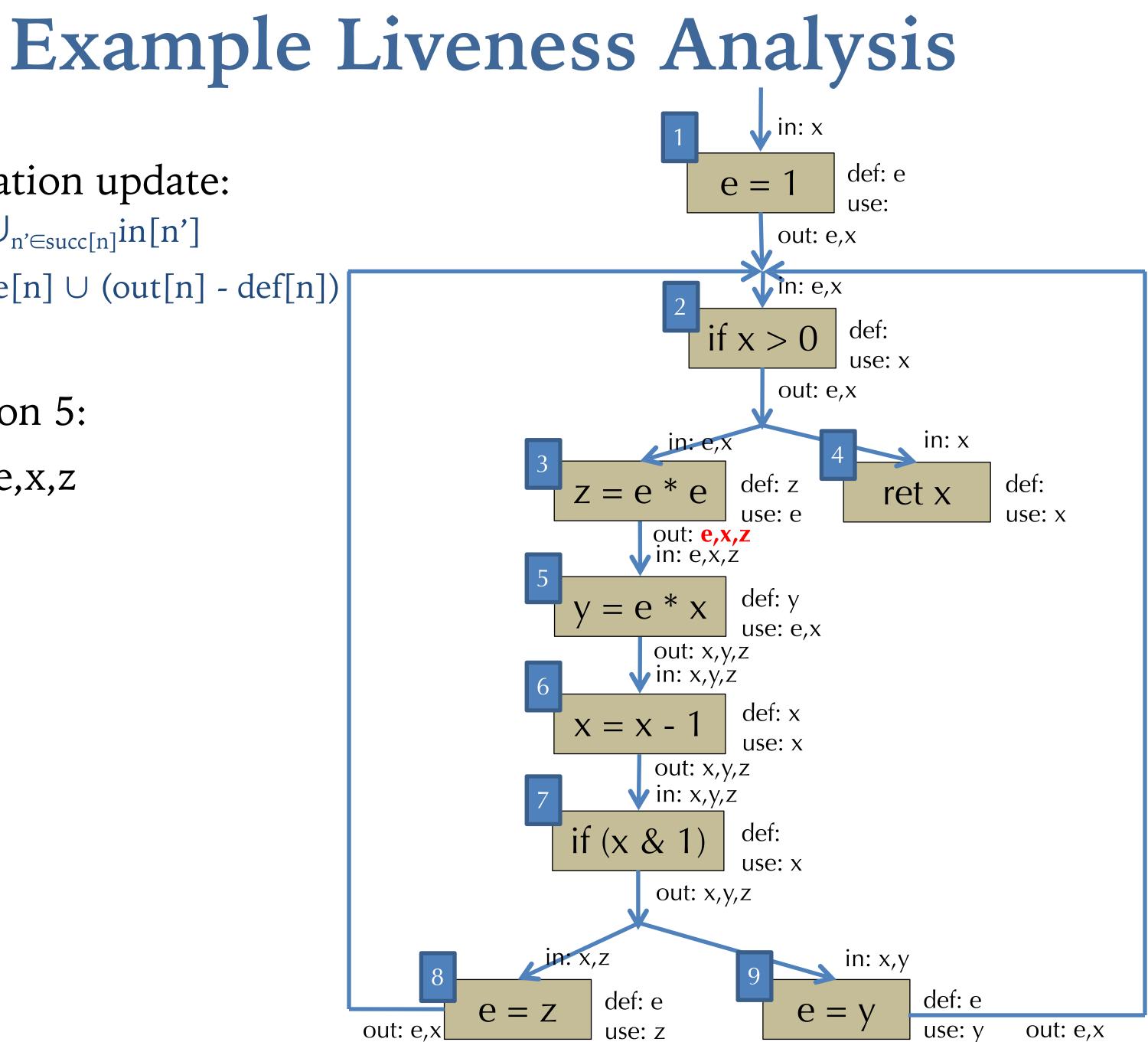
Iteration 4: \bullet out[5] = x,y,zin[5] = e,x,z



Iteration 5: ulletout[3] = e,x,z

Done!

out: e,x

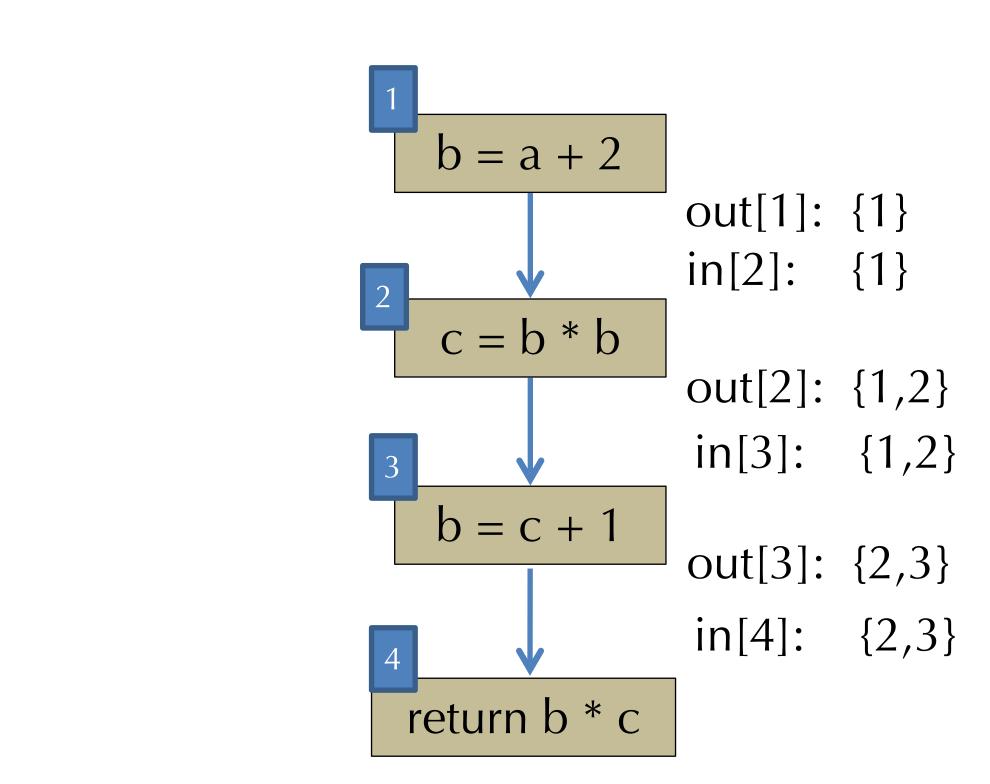




Reaching Definitions

Example of Reaching Definitions

•



Results of computing reaching definitions on this simple CFG:

Reaching Definitions Step 1

- Define the sets of interest for the analysis lacksquare
 - Let defs[a] be the set of *nodes* (statements) that define the variable a •
- Define gen[n] and kill[n] as follows: \bullet

•	Quadruple forms n:	gen[n]	kill[
	a = b op c	{n}	defs
	a = load b	{n}	defs
	store b, a	Ø	Ø
	$a = f(b_1,, b_n)$	{n}	defs
	f(b ₁ ,,b _n)	Ø	Ø
	br L	Ø	Ø
	braL1 L2	Ø	Ø
	return a	Ø	Ø

lacksquare

[n] $s[a] - \{n\}$

s[a] - {n}

 $s[a] - \{n\}$

gen[n] are node's definitions; kill[n] are the nodes, whose definitions are "shadowed" by n

Reaching Definitions Step 2

- Define the constraints that a reaching definitions solution must satisfy.
- $out[n] \supseteq gen[n]$
- $in[n] \supseteq out[n']$ if n' is in pred[n]
 - "The definitions that reach the beginning of a node include those that reach the exit of its any predecessor"
- out[n] \cup kill[n] \supseteq in[n]

 - Equivalently: $out[n] \supseteq in[n] kill[n]$

"The definitions that reach the end of a node at least include the definitions generated by the node"

"The definitions that come in to a node either reach the end of the node or are killed by it."

Reaching Definitions Step 3

- Convert constraints to iterated update equations: •
 - $in[n] := \bigcup_{n' \in pred[n]} out[n']$
 - $out[n] := gen[n] \cup (in[n] kill[n])$
- Algorithm: initialise in[n] and out[n] to \emptyset • – Iterate the update equations until a fixed point is reached - Why does it terminate?
- The algorithm terminates because in [n] and out [n] increase only monotonically \bullet – At most to a maximum set that includes all variable definitions in the program
- •

The algorithm is *precise* because it finds the *smallest* sets that satisfy the constraints.

Available Expressions

- Idea: want to perform common subexpression elimination: • -a = x + 1 a = x + 1
 - When is it safe?
- (i.e., x hasn't been assigned). - "x+1" is an available expression
- Dataflow values:
 - in[n] = set of *nodes* whose values are available on entry to n
 - out[n] = set of*nodes*whose values are available on exit of n

Available Expressions

This transformation is safe if x+1 means computes the same value at both places

Available Expressions Step 1

- Define the sets of values ullet
- Define gen[n] and kill[n] as follows: •
 - Quadruple forms n: gen[n] ullet $\{n\}$ - kill[n] a = b op ca = load b $\{n\}$ - kill[n] store b, a Ø
 - br L Ø br a L1 L2 Ø
 - $a = f(b_1, ..., b_n)$ Ø

$$f(b_1,...,b_n)$$
Øreturn aØ

- gen[n] node itself represents new available expression
- kill[n] nodes whose expressions no longer available after n

• Let uses [a] be the set of *nodes* that use the variable a in their expressions

```
kill[n]
uses a
uses [a]
                      Note the need for
                      "may alias" information...
uses[[x]]
(for all x that may equal a)
\emptyset
Ø
uses[a] \cup uses[[x]]
     (for all x)
                              Note that functions are
                 (for all x)
uses[[x]]
                              assumed to be impure...
Ø
```



Available Expressions Step 2

- Define the constraints that an available expressions solution must satisfy. •
- $out[n] \supseteq gen[n]$
 - "The expressions made available by n that reach the end of the node"
- $in[n] \subseteq out[n']$ if n' is in pred[n]
 - every predecessor"
- out[n] \cup kill[n] \supseteq in[n]

 - Equivalently: $out[n] \supseteq in[n] kill[n]$

• "The expressions available at the beginning of a node include those that reach the exit of

"The expressions available on entry either reach the end of the node or are killed by it."

Note similarities and differences with constraints for "reaching definitions".

Available Expressions Step 3

- Convert constraints to iterated update equations:
 - $in[n] := \bigcap_{n' \in pred[n]} out[n']$
 - $out[n] := gen[n] \cup (in[n] kill[n])$
- Unlike previous algorithms, this one is "shrinking" the set of desired facts
- Algorithm: initialise in[n] and out[n] to {set of all nodes}
 - Iterate the update equations until a fixed point is reached
 - Why does the algorithm terminate?
- The algorithm terminates because in [n] and out [n] decrease only monotonically
 - At most to a minimum of the empty set

The algorithm is precise because it finds the *largest* sets that satisfy the constraints.

General Dataflow Analysis Framework

Comparing Dataflow Analyses

- Look at the update equations in the inner loop of the analyses
- Liveness:
 - Let gen[n] = use[n] and kill[n] = def[n]
 - $out[n] := U_{n' \in succ[n]}in[n']$
 - $in[n] := gen[n] \cup (out[n] kill[n])$
- Reaching Definitions:
 - $in[n] := \bigcup_{n' \in pred[n]} out[n']$
 - $out[n] := gen[n] \cup (in[n] kill[n])$
- Available Expressions:
 - $in[n] := \bigcap_{n' \in pred[n]} out[n']$
 - $out[n] := gen[n] \cup (in[n] kill[n])$

(backward)

(forward)

(forward)

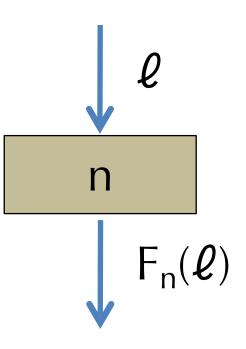
Common Features

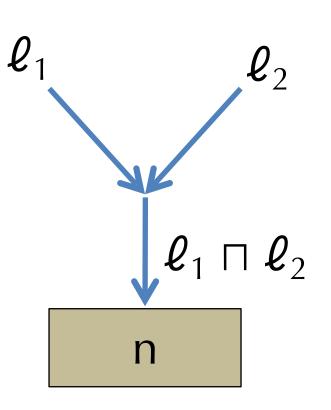
- All of these analyses have a *domain* over which they solve constraints. •
 - Liveness, the domain is sets of variables – Reaching defns., Available exprs. the domain is sets of nodes
- Each analysis has a notion of gen[n] and kill[n] ullet- Used to explain how information *propagates* across a node: what is added, what is removed.
- Each analysis is propagates information either forward or backward ullet- Forward: in[n] defined in terms of predecessor nodes' out[]
- Backward: out[n] defined in terms of successor nodes' in[]
- Each analysis has a way of aggregating (combining) information from in/out flow • – Liveness & reaching definitions take union (\cup)
- - Available expressions uses intersection (\cap)
 - Union expresses a property that holds for *some* path (existential)
 - Intersection expresses a property that holds for *all* paths (universal)

(Forward) Dataflow Analysis Framework

A forward dataflow analysis can be characterized by:

- A domain of dataflow values \mathcal{L}
 - e.g. $\int f$ = the powerset of all variables
 - Think of $\ell \in \mathcal{L}$ as a property, then " $z \in \ell$ " means "z has the property"
- 2. For each node n, a *flow function* $F_n : \mathcal{L} \to \mathcal{L}$
 - So far we've seen $F_n(\ell) = gen[n] \cup (\ell kill[n])$
 - So: $out[n] = F_n(in[n])$
 - "If ℓ is a property that holds before the node n, then $F_n(\ell)$ holds after n"
- A *combining* operator ⊓ 3.
 - "If we know either ℓ_1 or ℓ_2 holds on entry to node n, we know at most $\ell_1 \sqcap \ell_2$ "
 - $in[n] := \prod_{n' \in pred[n]} out[n']$





Generic Iterative (Forward) Analysis

repeat until no change for all n

- $in[n] := \prod_{n' \in pred[n]} out[n']$ $out[n] := F_n(in[n])$

end

end

- Here, $\top \in \mathcal{L}$ ("top") represents having the "maximum" amount of information. – Having "more" information enables more optimizations "Maximum" amount could be inconsistent with the constraints, so we can't keep it. :-(– Iteration refines the answer, eliminating inconsistencies

- for all n, $in[n] := \top$, $out[n] := \top$

Structure of \mathcal{L}

- The domain has structure that reflects the "amount" of information for each dataflow value.
- Some dataflow values are more informative than others:
 - Write $\ell_1 \subseteq \ell_2$ whenever ℓ_2 provides at least as much information as ℓ_1 .
 - The dataflow value ℓ_2 is "better" for enabling optimizations.
- Example 1: for available expressions analysis, larger sets of nodes are more informative. - Having a larger set of nodes (equivalently, expressions) available means that there is more opportunity for
- common subexpression elimination.
 - So: $\ell_1 \subseteq \ell_2$ if and only if $\ell_1 \subseteq \ell_2$
- Example 2: for liveness analysis, *smaller* sets of variables are more informative. – Having smaller sets of variables live across an edge means that there are fewer conflicts
 - for register allocation assignments.
 - So: $\ell_1 \sqsubseteq \ell_2$ if and only if $\ell_1 \supseteq \ell_2$



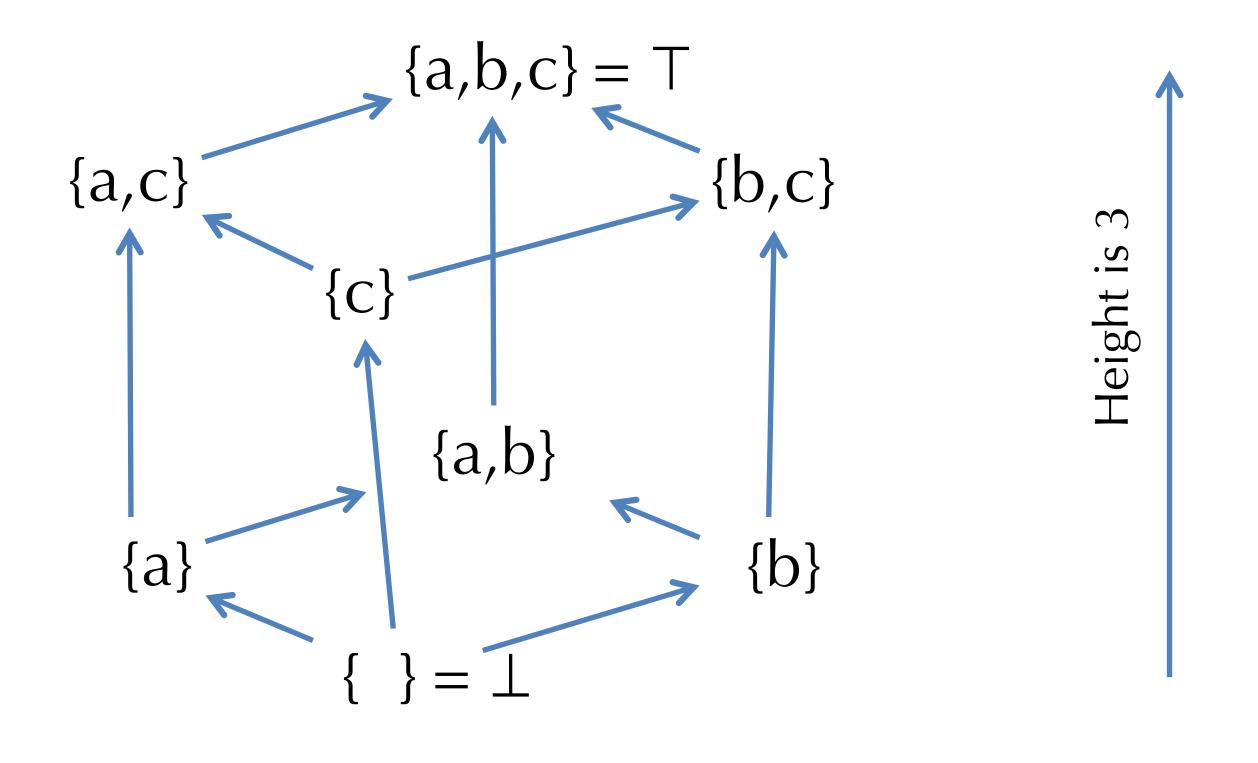
Las a Partial Order

- \mathcal{L} is a *partial order* defined by the ordering relation \sqsubseteq .
- A partial order is an ordered set.
- Some of the elements might be *incomparable*.
 That is, there might be ℓ₁, ℓ₂ ∈ L such that neither ℓ₁ ⊑ ℓ₂ nor ℓ₂ ⊑ ℓ₁
- Properties of a partial order:
 - Reflexivity: $\ell \sqsubseteq \ell$
 - *Transitivity*: $\boldsymbol{\ell}_1 \sqsubseteq \boldsymbol{\ell}_2$ and $\boldsymbol{\ell}_2 \sqsubseteq \boldsymbol{\ell}_3$ implies $\boldsymbol{\ell}_1 \sqsubseteq \boldsymbol{\ell}_2$
 - Anti-symmetry: $\ell_1 \sqsubseteq \ell_2$ and $\ell_2 \sqsubseteq \ell_1$ implies $\ell_1 = \ell_2$
- Examples:
 - Integers ordered by \leq
 - Types ordered by <:
 - Sets ordered by \subseteq or \supseteq

Subsets of $\{a,b,c\}$ ordered by \subseteq

 $\begin{array}{c} \boldsymbol{\ell}_2 \\ \uparrow & \boldsymbol{\ell}_1 & \sqsubseteq & \boldsymbol{\ell}_2 \\ \boldsymbol{\ell}_1 \end{array}$

Partial orders are often presented as a Hasse diagram.



order ⊑ is ⊆

meet ⊓ is ∩ joir

join L is U

- The *combining* operator \sqcap is called the "meet" operation.
- It constructs the greatest lower bound: •
 - $-\ell_1 \sqcap \ell_2 \sqsubseteq \ell_1$ and $\ell_1 \sqcap \ell_2 \sqsubseteq \ell_2$ "the meet is a lower bound"
 - If $\ell \subseteq \ell_1$ and $\ell \subseteq \ell_2$ then $\ell \subseteq \ell_1 \sqcap \ell_2$ "there is no greater lower bound"
- Dually, the \sqcup operator is called the "join" operation. •
- It constructs the *least upper bound*: ullet
 - $-\ell_1 \sqsubseteq \ell_1 \sqcup \ell_2$ and $\ell_2 \sqsubseteq \ell_1 \sqcup \ell_2$ "the join is an upper bound"
 - If $\ell_1 \sqsubseteq \ell$ and $\ell_2 \sqsubseteq \ell$ then $\ell_1 \sqcup \ell_2 \sqsubseteq \ell$ "there is no smaller upper bound"
- A partial order that has all meets and joins is called a *lattice*. ullet– If it has just meets, it's called a meet semi-lattice.

Meets and Joins

Another Way to Describe the (Forward) Algorithm

- Algorithm repeatedly computes (for each node n):
 - $out[n] := F_n(in[n])$
- Equivalently: $out[n] := F_n(\prod_{n' \in pred[n]} out[n'])$ By definition of in[n]
- Let $x_n = out[n]$

 - $\mathbf{F}(\mathbf{X}) = (F_1(\prod_{i \in pred[1]} out[j]), F_2(\prod_{i \in pred[2]} out[j]), ..., F_n(\prod_{i \in pred[n]} out[j]))$
- Any solution to the constraints is a *fixpoint* **X** of **F** - i.e. F(X) = X

We can write this as a simultaneous update of the vector of out[n] values:

- Let $X = (x_1, x_2, ..., x_n)$ it's a vector of points in \mathcal{L} corresponding to CFG nodes



Iteration Computes Fixpoints

- Let $\mathbf{X}_0 = (\top, \top, ..., \top)$
- Each loop through the algorithm apply **F** to the old vector: • $\mathbf{X}_1 = \mathbf{F}(\mathbf{X}_0)$ $\mathbf{X}_2 = \mathbf{F}(\mathbf{X}_1)$

 $\mathbf{F}^{k+1}(\mathbf{X}) = \mathbf{F}(\mathbf{F}^{k}(\mathbf{X}))$ ullet

• • •

- A fixpoint is reached when $F^k(X) = F^{k+1}(X)$ •
 - That's when the algorithm stops.
- Wanted: a maximal fixpoint \bullet

– Because that one is more informative/useful for performing optimizations

Monotonicity & Termination

- Each flow function F_n maps lattice elements to lattice elements; to be sensible is should be monotonic: ullet
- $F: \mathcal{I} \to \mathcal{I}$ is monotonic iff: $\ell_1 \sqsubseteq \ell_2$ implies that $F(\ell_1) \sqsubseteq F(\ell_2)$ - Intuitively: "If you have more information entering a node, then you have more information leaving the node."
- Monotonicity lifts point-wise to the function: $\mathbf{F}: \mathcal{L}^n \to \mathcal{L}^n$ \bullet - vector $(x_1, x_2, \dots, x_n) \sqsubseteq (y_1, y_2, \dots, y_n)$ iff $x_i \sqsubseteq y_i$ for each i
- Note that **F** is consistent: $F(X_0) \sqsubseteq X_0$ ullet

– So each iteration moves at least one step down the lattice (for some component of the vector) $- \ldots \sqsubseteq \mathsf{F}(\mathsf{F}(\mathsf{X}_0)) \sqsubseteq \mathsf{F}(\mathsf{X}_0) \sqsubseteq \mathsf{X}_0$

Therefore, # steps needed to reach a fixpoint is at most the height H of \mathcal{L} times the number of nodes: $O(H_n)$ — height of the lattice

More on Fixpoint Solutions

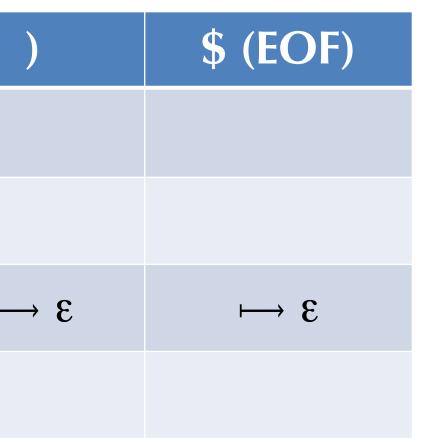
Remember constructing LL(1) parse tables ullet

$T \mapsto S$
$S \mapsto ES'$
$S' \mapsto \epsilon$
$S' \mapsto + S$
$E \mapsto number \mid (S)$

- First(T) = First(S)
- First(S) = First(E)
- $First(S') = \{ + \}$
- First(E) = { number, '(' }
- Follow(S') = Follow(S)

	number	+	(
Т	\mapsto S\$		⊢→S\$	
S	$\mapsto E S'$		⊢→E S′	
S'		\mapsto + S		F
E	⊢ num.		\mapsto (S)	

• Follow(S) = { \$, ')' } \cup Follow(S')



Then: we want the *least* solution to this system of set equations... a fixpoint computation. More on these later in the course.

Now: This solution is obtained by starting from taking all First/Follow as \emptyset and then iterating the equations until *fixpoint* is reached.



Dataflow Analysis: Summary

- Many dataflow analyses fit into a common framework. •
- Key idea: *iterative solution* of a system of equations (constraints) over a *lattice* of *facts*. • - Iteration terminates if flow functions are *monotonic*.

 - Solution is obtained as the greatest fixpoint is reached via the meet operation (\Box) .
- In the literature, sometimes the definition of the analysis lattice is reversed: • – The most useful/precise information is represented by the bottom element (\bot) - Solution is obtained as the *least* fixpoint via iterative application of *join* operator (\sqcup) – The two definitions are equivalent modulo the (semi-)lattice *direction*.

Implementation

- See HW6 lacksquare
 - Generic analysis is to be defined in solver.ml Control-Flow Graphs are defined in cfg.ml
 - lacksquareullet
- Analysis example: liveness.ml •
- Printing analysis results, e.g., liveness: ullet

./printanalysis.native -live llprograms/analysis2.ll

Let's have a short break

Register Allocation

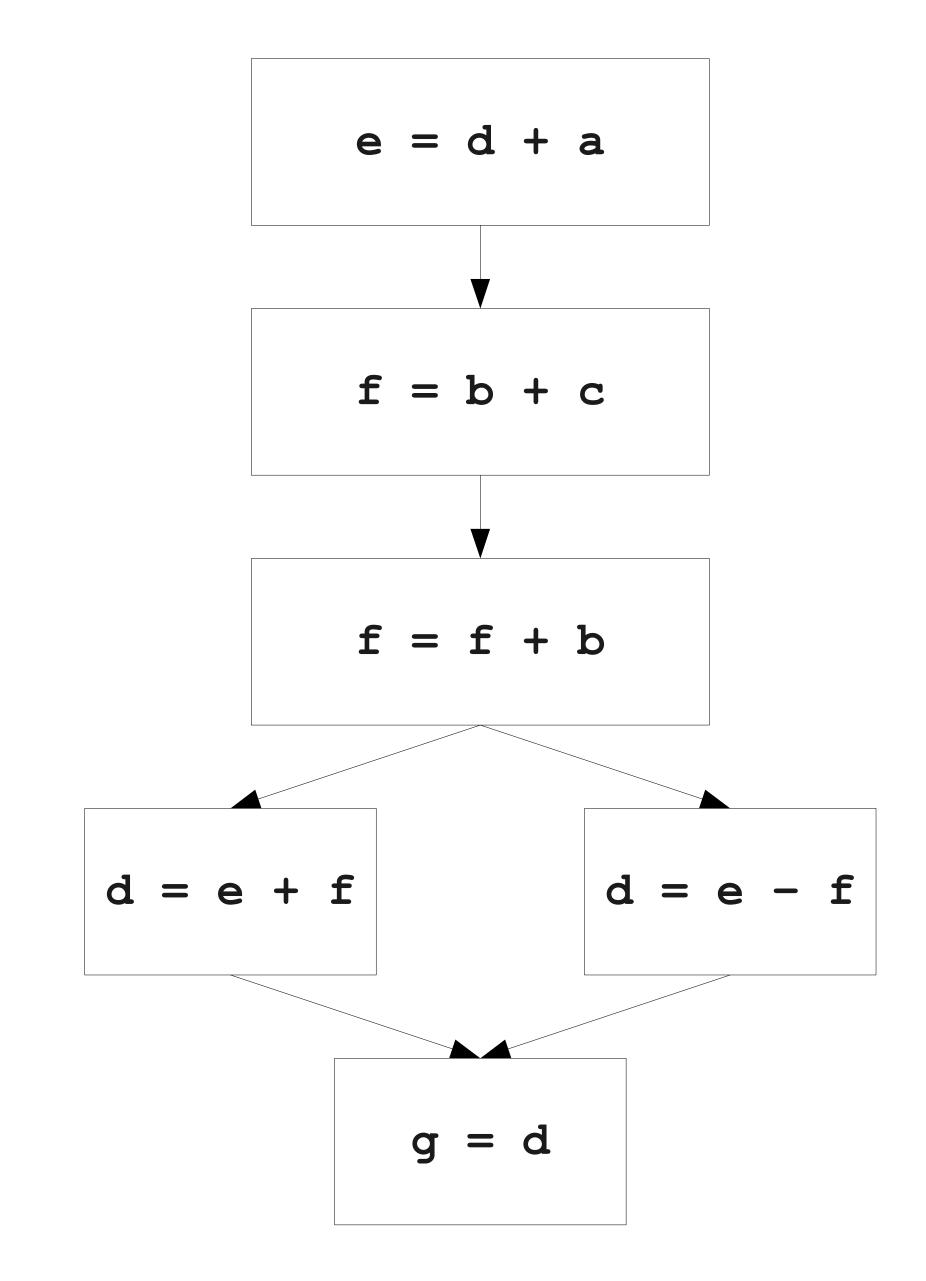
Register Allocation Problem

- Given: an IR program that uses
 e.g. the uids of our LLVM programs
- Find: a mapping from temporaries to machine registers such that
 - program semantics is preserved (i.e. the behaviour is the same)
 - register usage is maximised
 - moves between registers are minimised
 - calling conventions / architecture requirements are obeyed
- Stack Spilling
 - If there are k registers available and m > k temporaries are *live* at the same time, then not all of them will fit into registers.
 - So: "spill" the excess temporaries to the stack.

• Given: an IR program that uses an unbounded number of temporaries

Linear-Scan Register Allocation

	е	-	d	+	a	
	f	=	b	+	С	
	f	=	f	+	b	
	I	EZ	е	Go	oto	_L0
	d	=	е	+	f	
	Go	oto	>_	_L]	L;	
_L0 :	•					
	d		е	-	f	
_L1 :						
	g	=	d			



Linear-Scan Register Allocation



e = d + a		
f = b + c		
f = f + b		
IfZ e Goto LO		
d = e + f		
Goto _L1;		
_L0:		
d = e - f		
_L1:		
g = d		

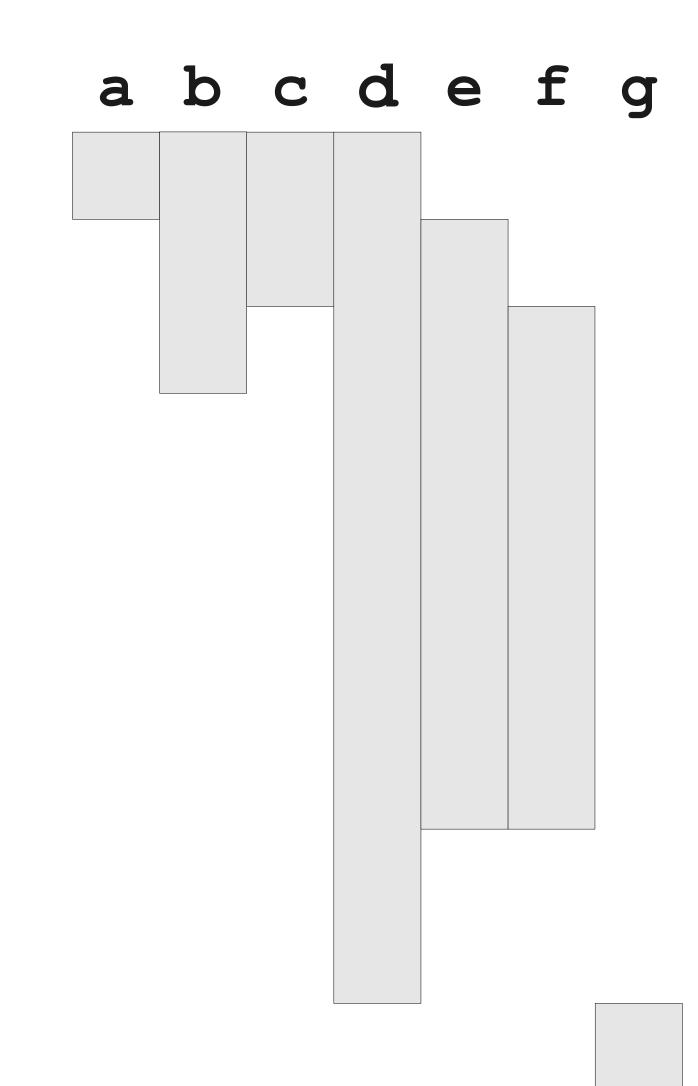
{ a, b, c, d } e = d + a{ b, c, e } { b, c, e } f = b + c{ b, e, f} { b, e, f } f = f + b{ e, f } { e, f } { e, f } d = e - fd = e + f{ d } { d } { d } g = d{ g }

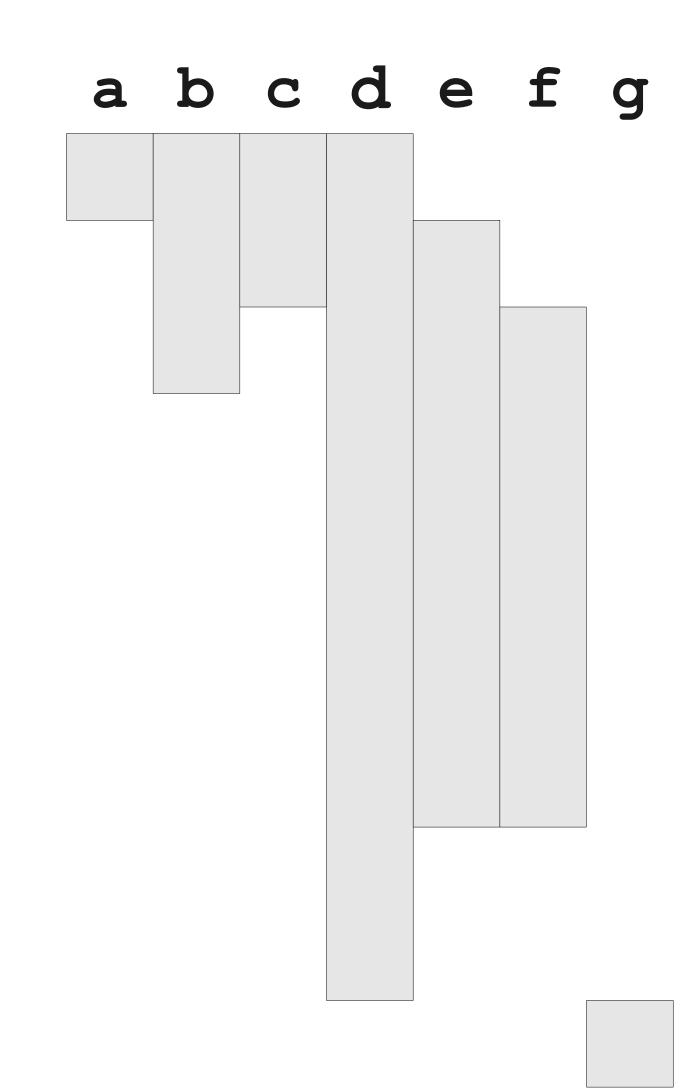


Idea: sweep the program *top-down*, allocating registers for *live* variables and *evicting* non-live ones.

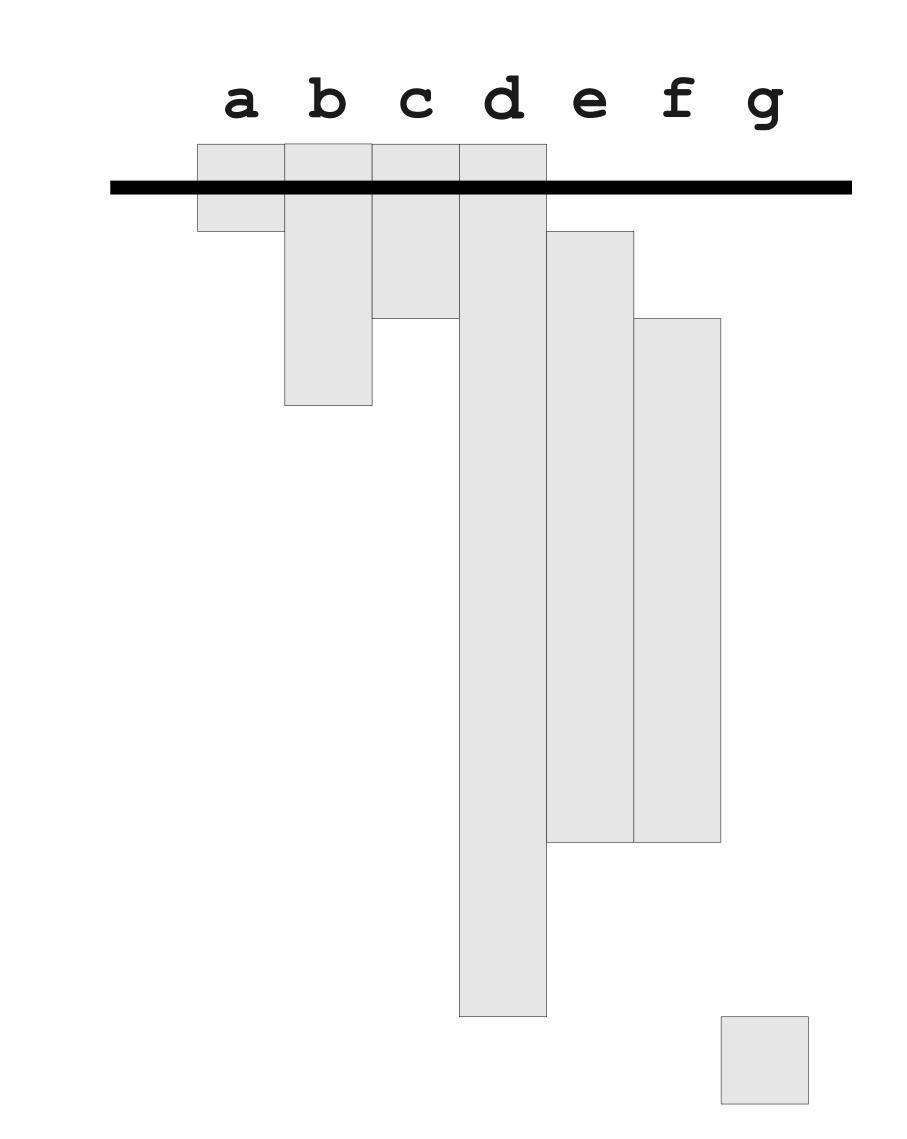
Linear-Scan Register Allocation

Linear-Scan Register Allocation



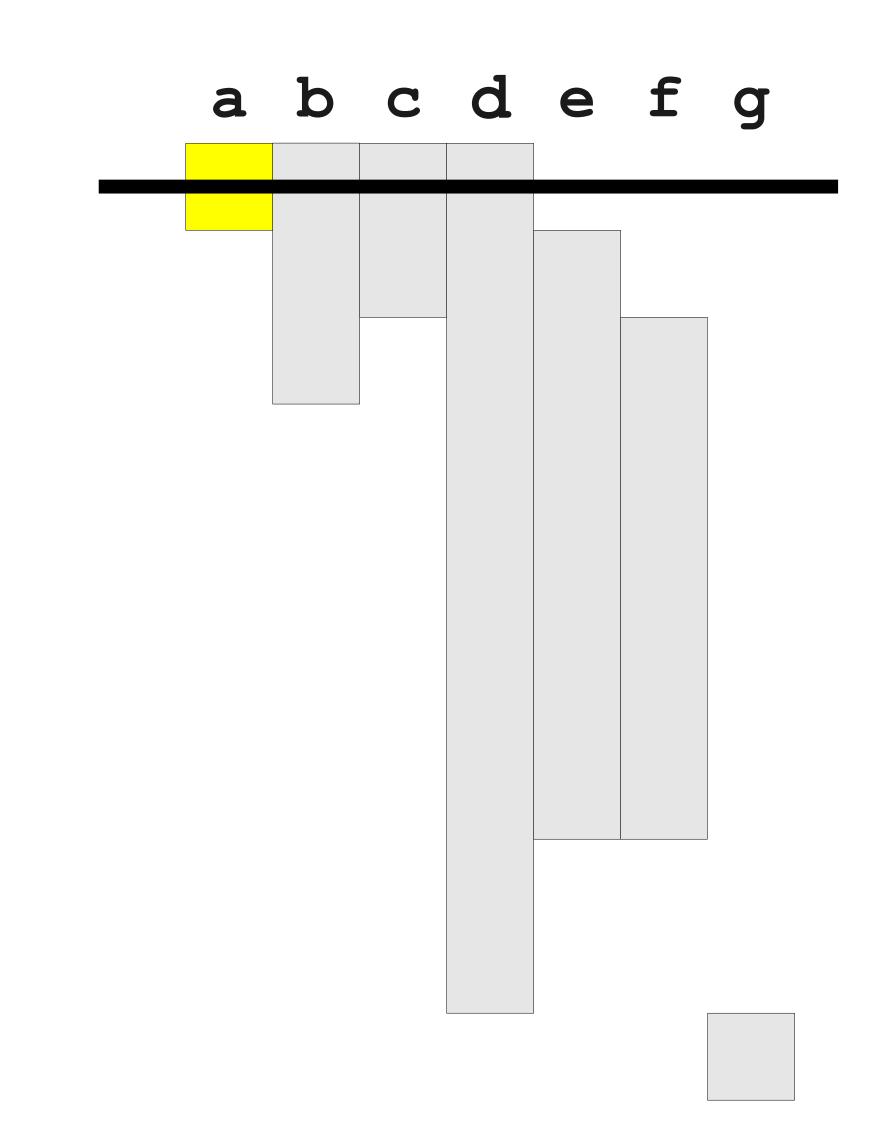




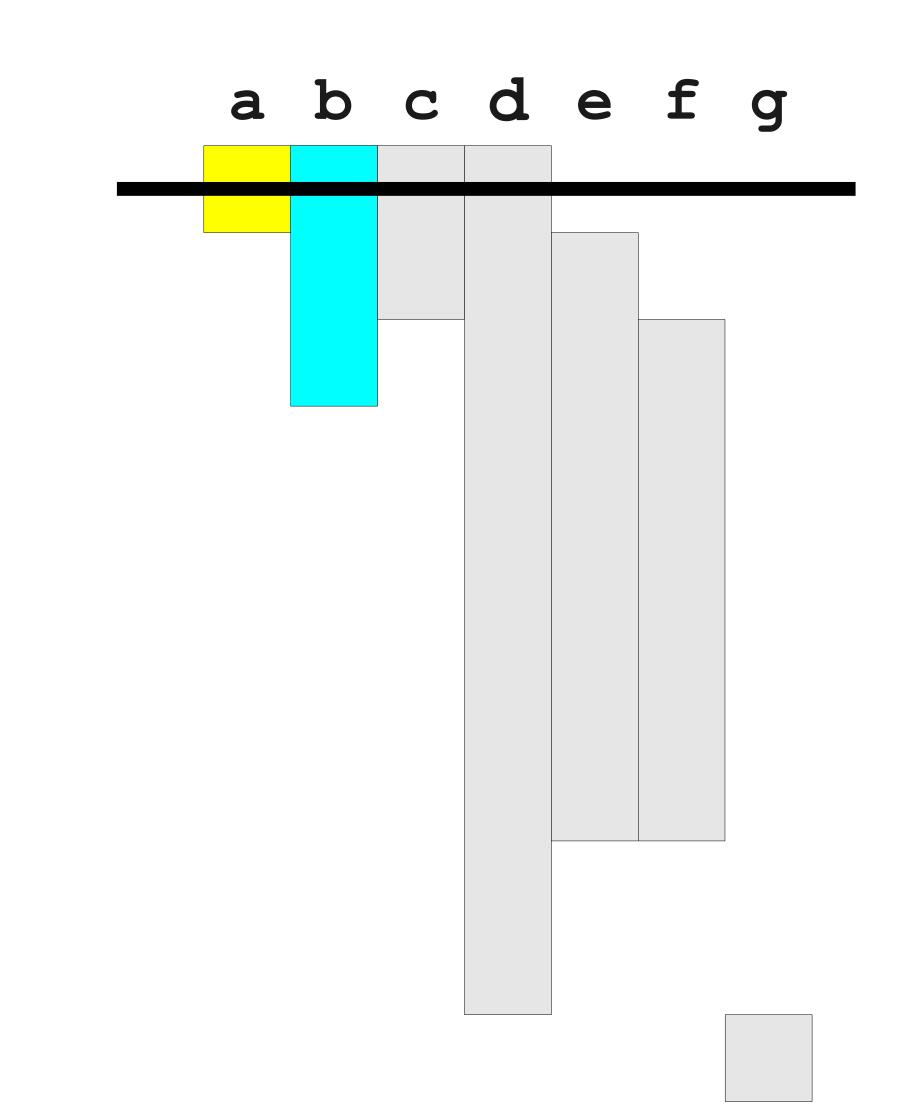




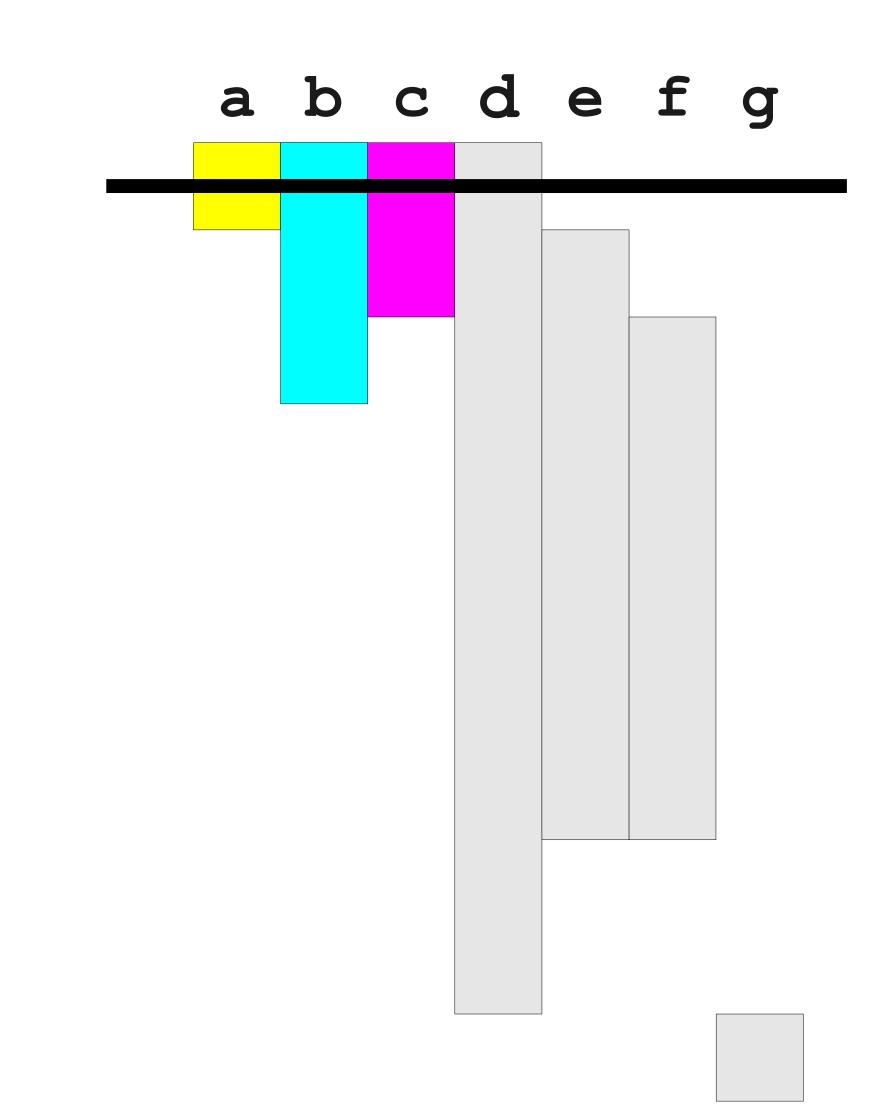
Free Registers R₀ R₁ R₂ R₂



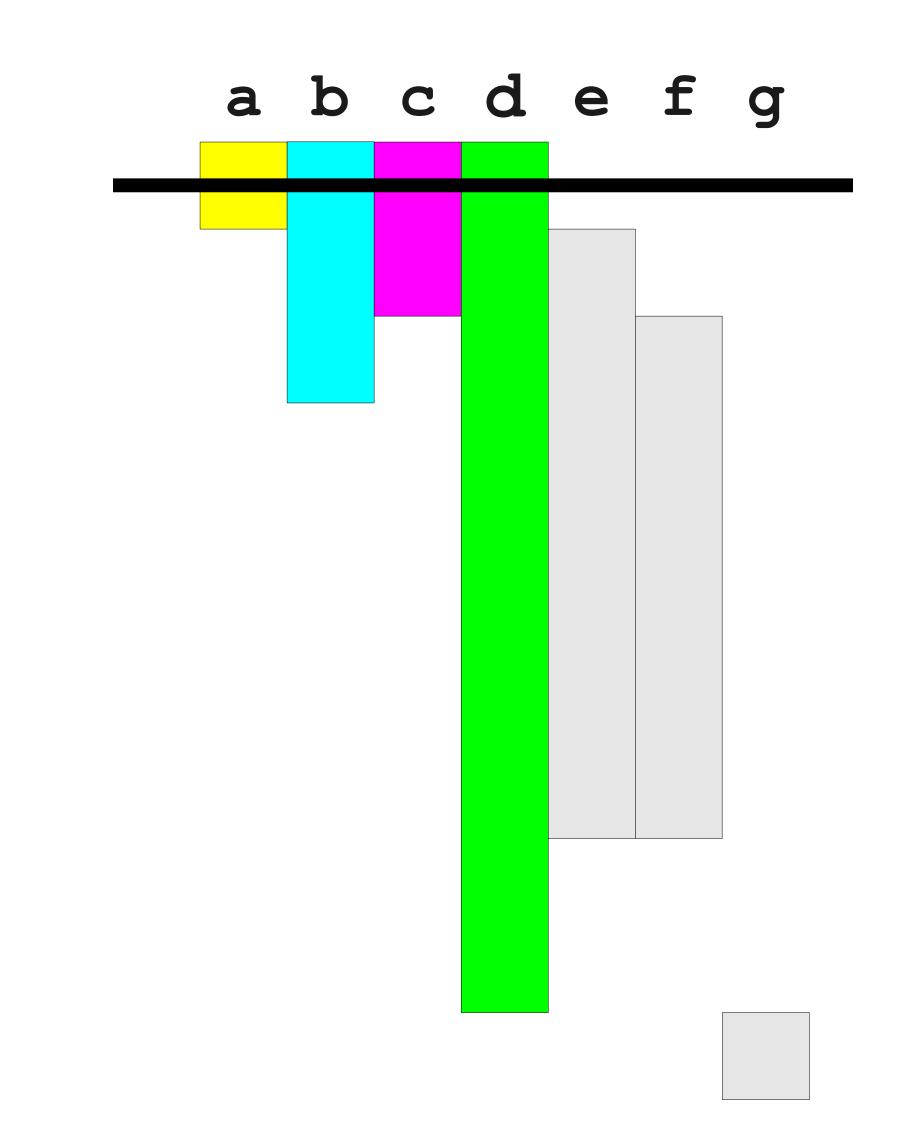






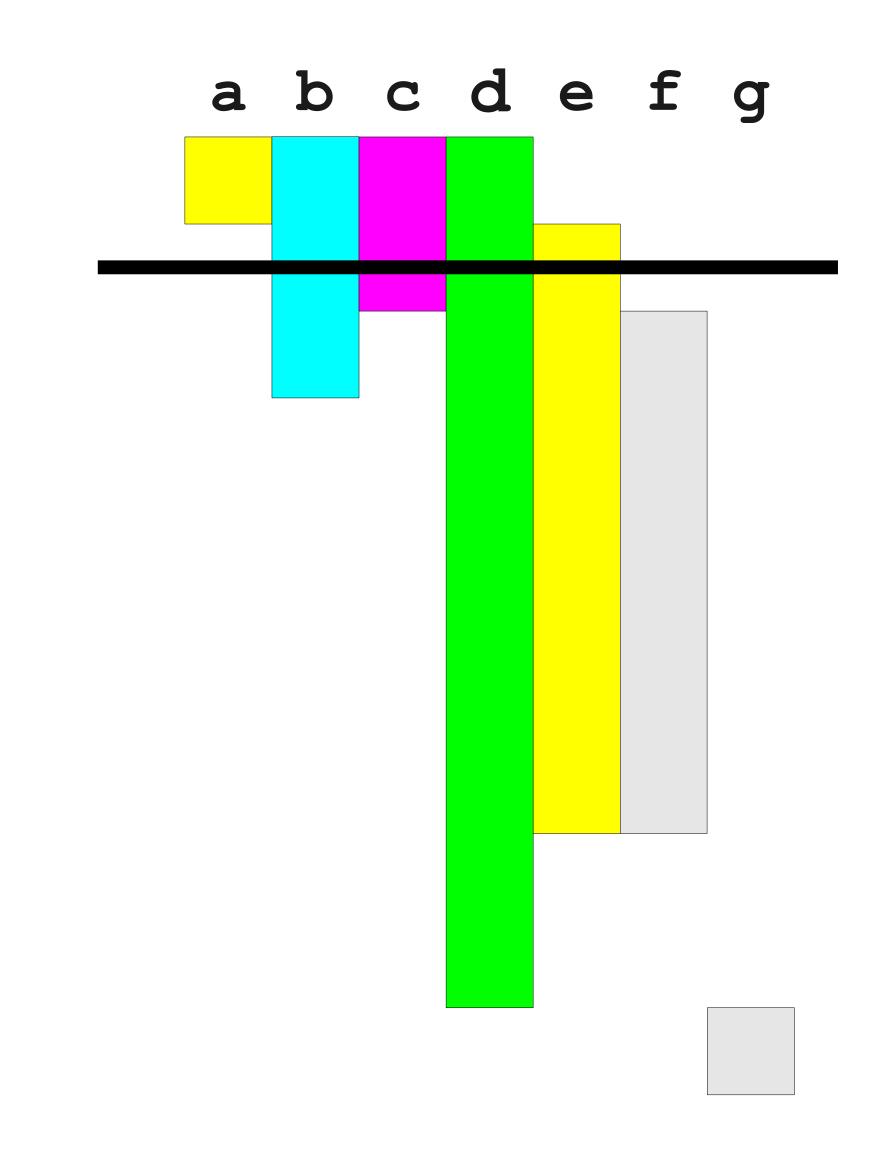






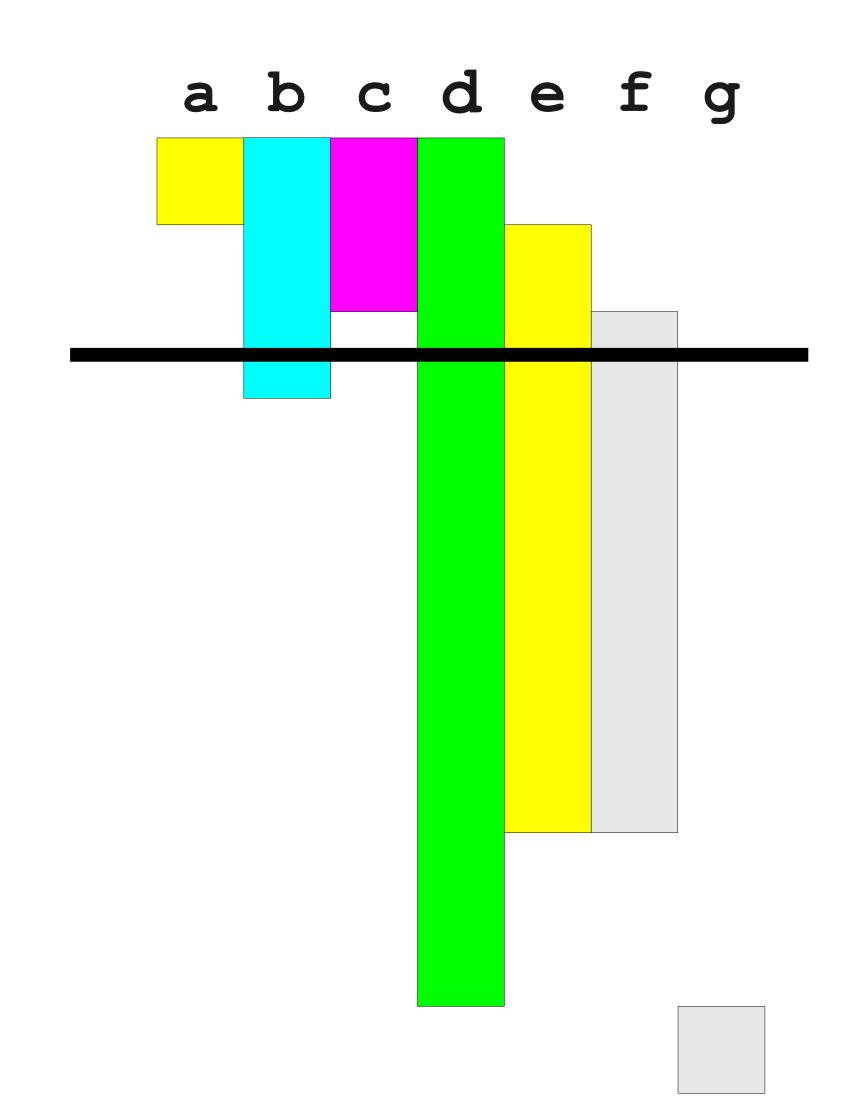


Free Registers R₂ R, R₂ R

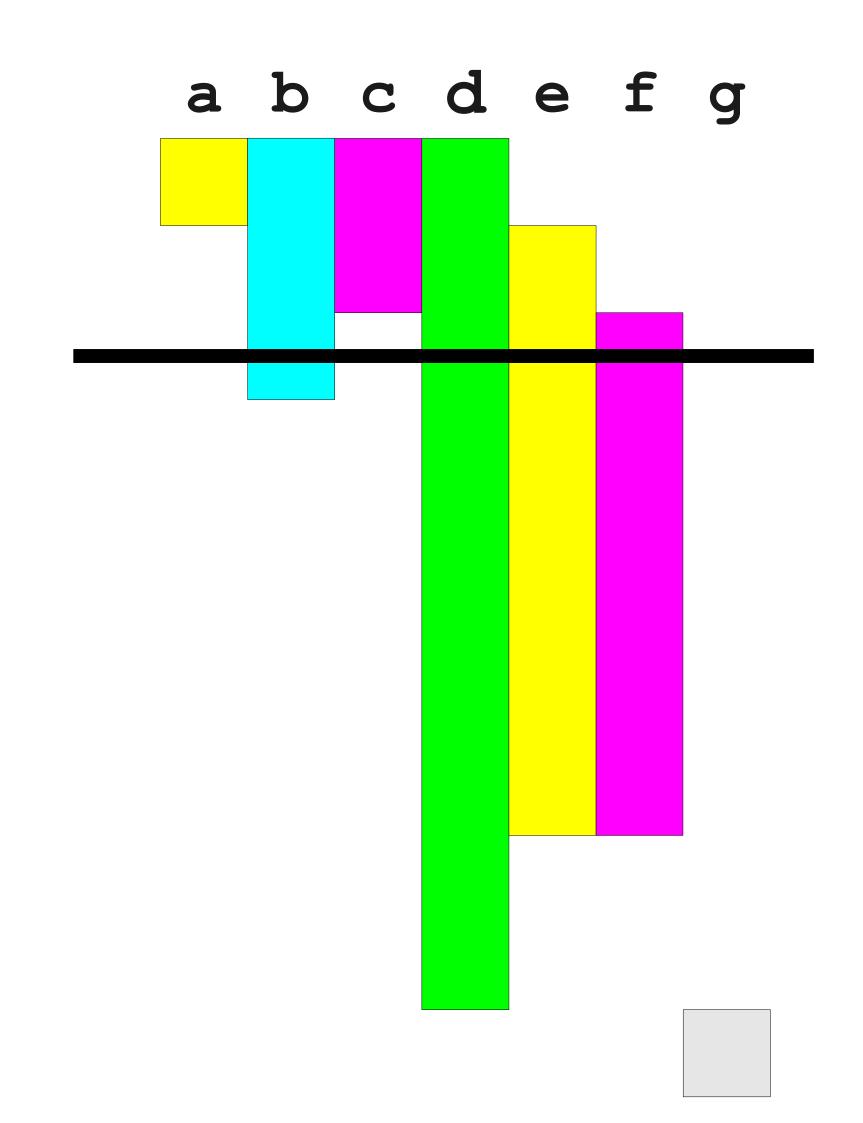




Free Registers R₁ \mathbf{R}_{2} R₂ R

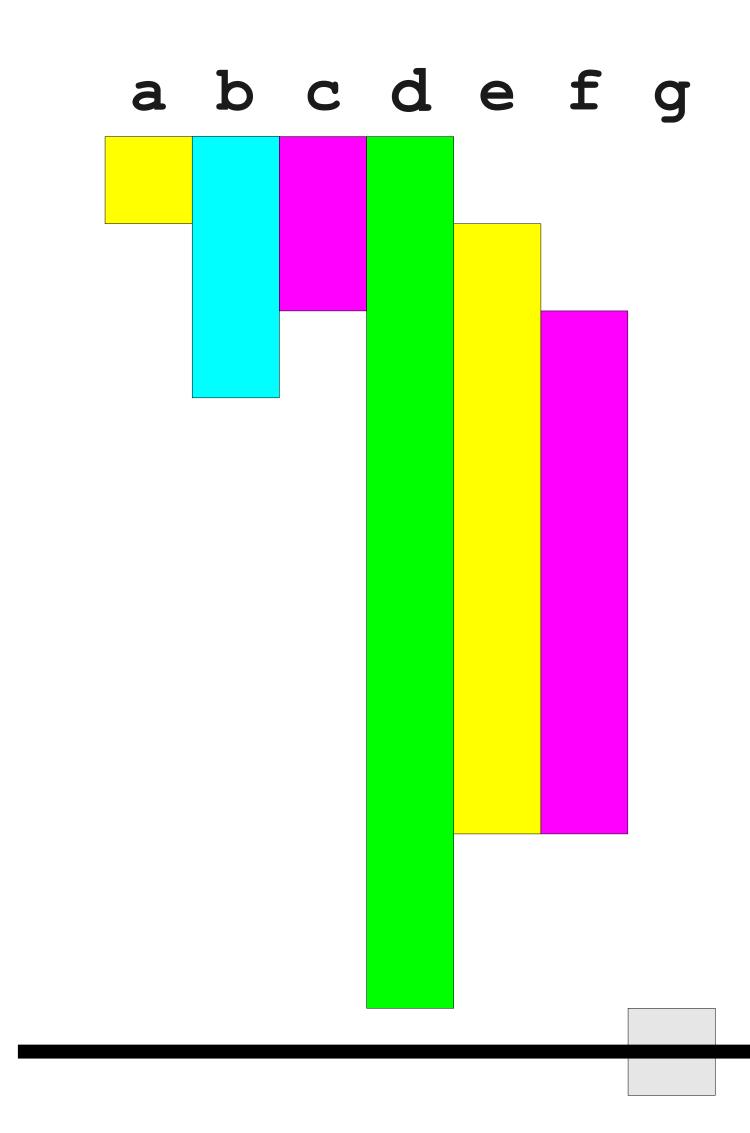






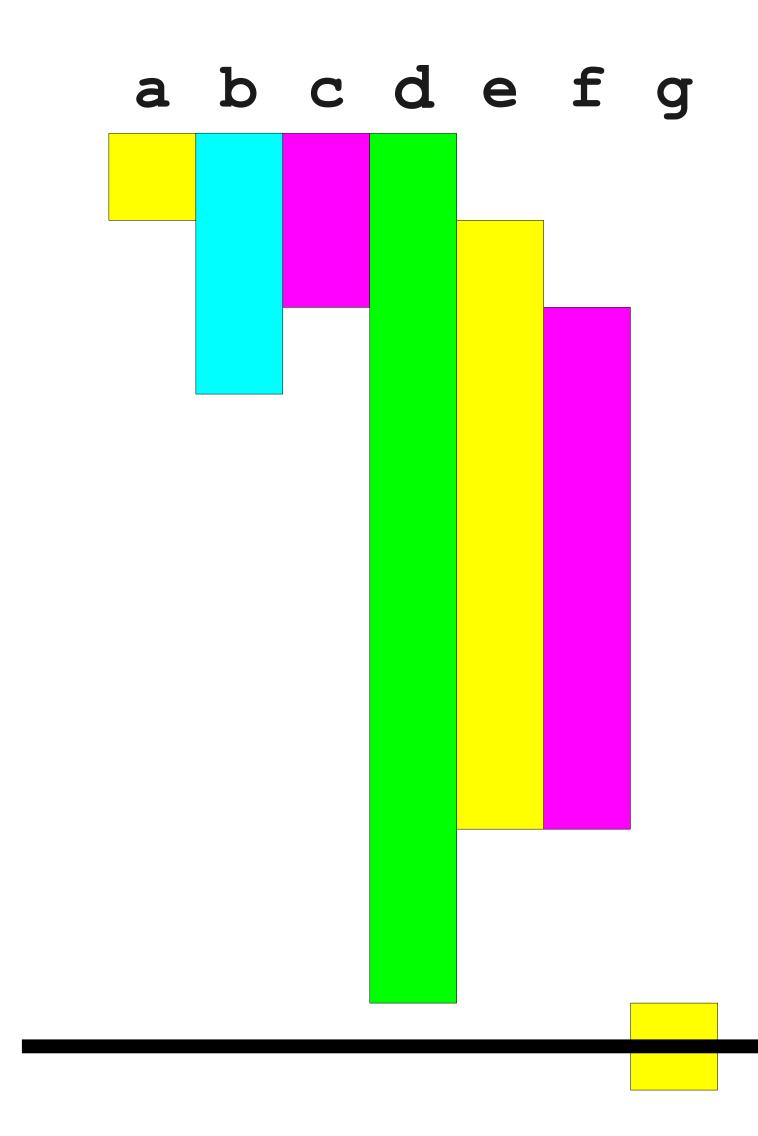


Free Registers R₁ \mathbf{R}_{2} R₂ R





Free Registers R₂ R₂ R₁ R₀





Linear-Scan Register Allocation

Simple, greedy register-allocation strategy:

- Compute liveness information: live(x)
 - recall: live(x) is the set of uids that are live on entry to x's definition
- 2. Let regs be the set of usable registers
 - usually reserve a couple for spill code (offloading to stack) [our implementation uses rax,rcx]
- Maintain "layout" uid loc that maps uids to locations 3.
 - locations include registers and stack slots n, starting at n=0
- 4. Scan through the program. For each instruction that defines a uid x
 - used = {r | reg r = uid loc(y) s.t. $y \in live(x)$ }
 - available = regs used
 - If available is empty: // no registers available, spill _

uid_loc(x) := slot n ; n = n + 1

// choose an available register - Otherwise, pick r in available: uid loc(x) := reg r

Linear-Scan Register Allocation

- Advantages

 - Very efficient (after computing live intervals, runs in linear time) – Produces good code in many instances.
 - Allocation step works in one pass; can generate code during iteration.
 - Often used in JIT compilers like Java HotSpot.
- Pitfalls \bullet

 - Doesn't always choose a very good strategy due to greediness. – Doesn't work well with branching.

Linear Scan and Branching

a = d = c = 0// live = { } b = 1// live = { b }
// live = { b } a = b + 1 d = b + 2// live = { d, b } // live = { a, b } c = a + bc = d + b// live = { d, c } // live = { a, c } print(a) print(d) // live = { c } // live = { c }

return c





Register Allocation via Colour Graphs

Basic process:

- Compute liveness information for each temporary (%uid). 1.
- Create an *interference graph*: 2.
 - Nodes are temporary variables (%uids). —
 - There is an *edge* between node **n** and **m** if **n** is *live* at the same time as **m**
- 3. Try to colour the graph
 - Each colour corresponds to a register
- 4.
- 5. Rewrite the program to use registers

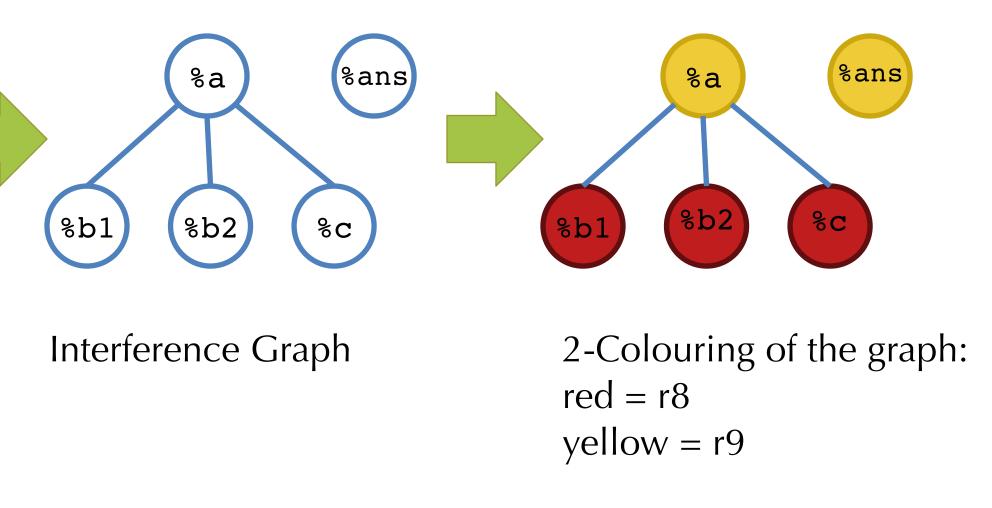
In case **Step 3** fails, "spill" a temporary to the stack and repeat the whole process.

Interference Graphs

- Nodes of the graph are %uids
- Edges connect variables that *interfere* with each other
 - ____ across which they are both live).
- Register assignment is a graph colouring.
 - A graph colouring assigns each node in the graph a colour (register) _____
 - Any two nodes connected by an edge must have different colours. —
- Example:

```
// live = \{\$a\}
8b1 = add i 32 8a, 2
// live = {a, 8b1}
%c = mult i32 %b1, %b1
// live = \{a, c\}
%b2 = add i32 %c, 1
// live = \{a, 8b2\}
%ans = mult i32 %b2, %a
// live = {%ans}
return %ans;
```

Two variables *interfere* if their live ranges intersect (i.e. there is an edge in the control-flow graph)



Register Allocation Questions

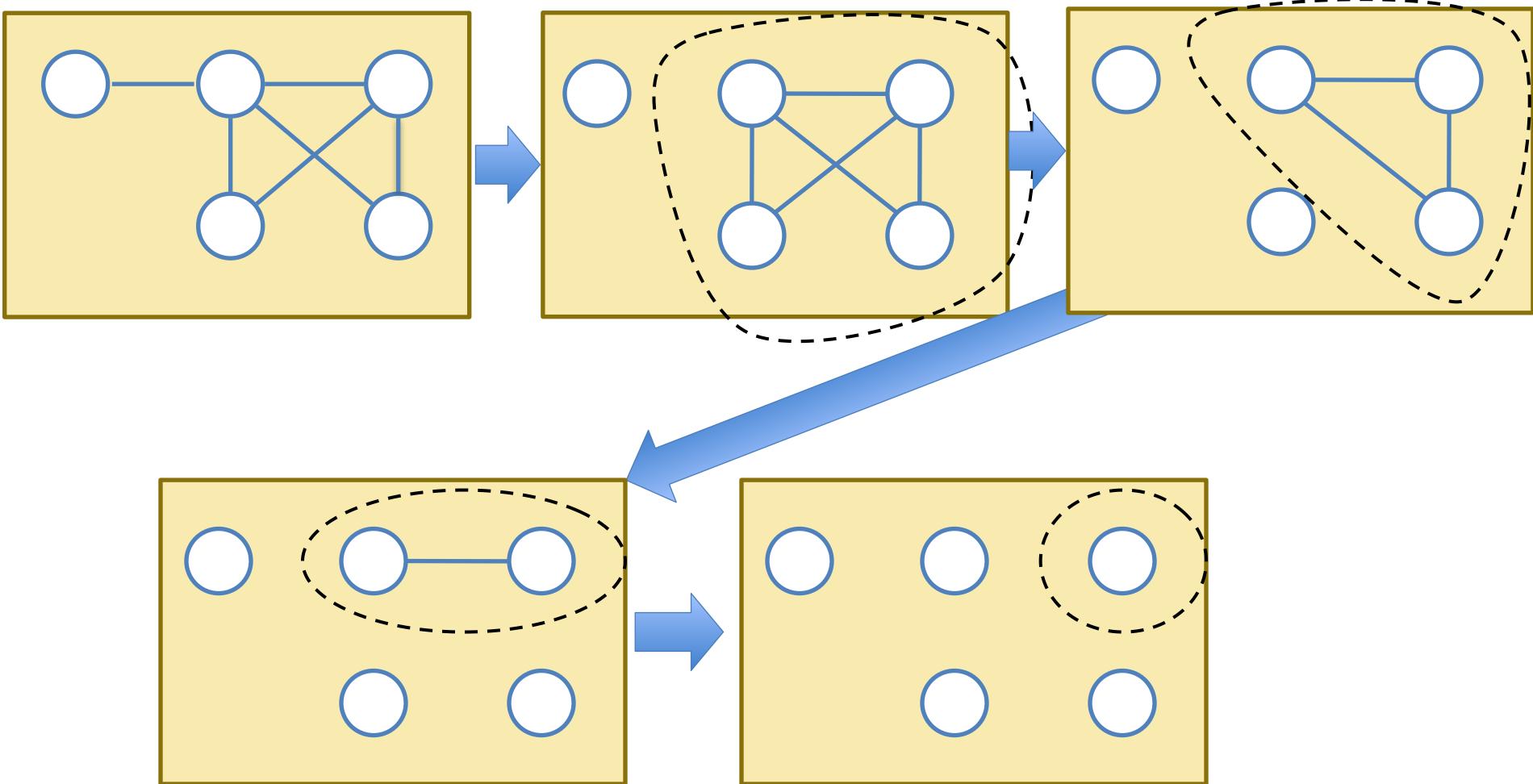
- Can we efficiently find a k-colouring of the graph whenever possible? – Answer: in general the problem is NP-complete (it requires search) But, we can do an efficient approximation using *heuristics*. ____

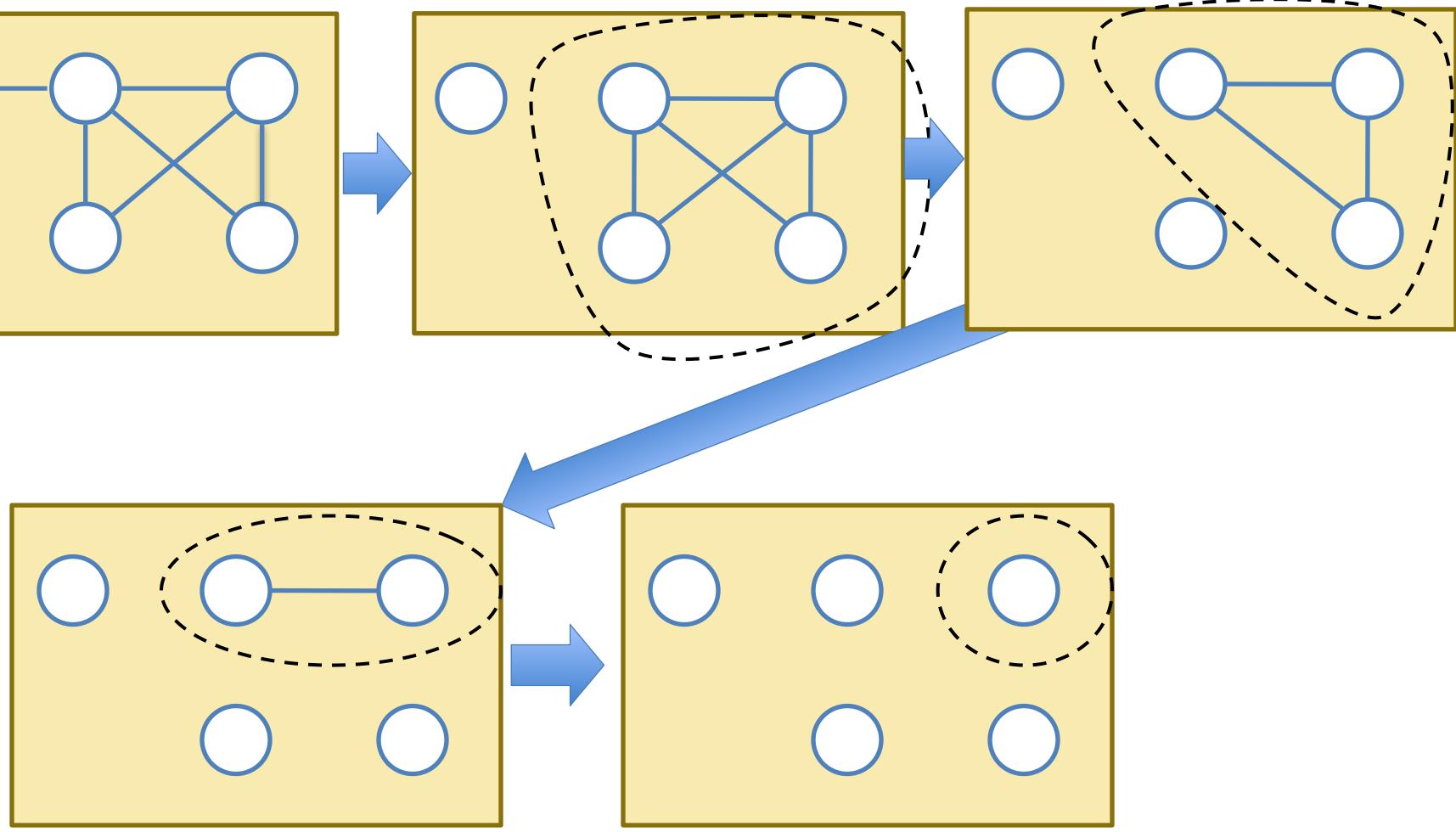
- How do we assign registers to colours? – If we do this in a smart way, we can eliminate many redundant MOV instructions.
- What do we do when there aren't enough colours/registers? We have to use stack space, but how do we do this effectively?

Colouring a Graph: Kempe's Algorithm

- Kempe [1879] provides this algorithm for K-coloring a graph.
- It's a recursive algorithm that works in three steps:
- Step 1: Find a node with degree < K and cut it out of the graph.
 - Remove the nodes and edges.
 - This is called *simplifying* the graph
- Step 2: Recursively K-colour the remaining subgraph
- Step 3: When remaining graph is coloured, there must be at least one free colour available for the deleted node (since its degree was < K). Pick such a colour.

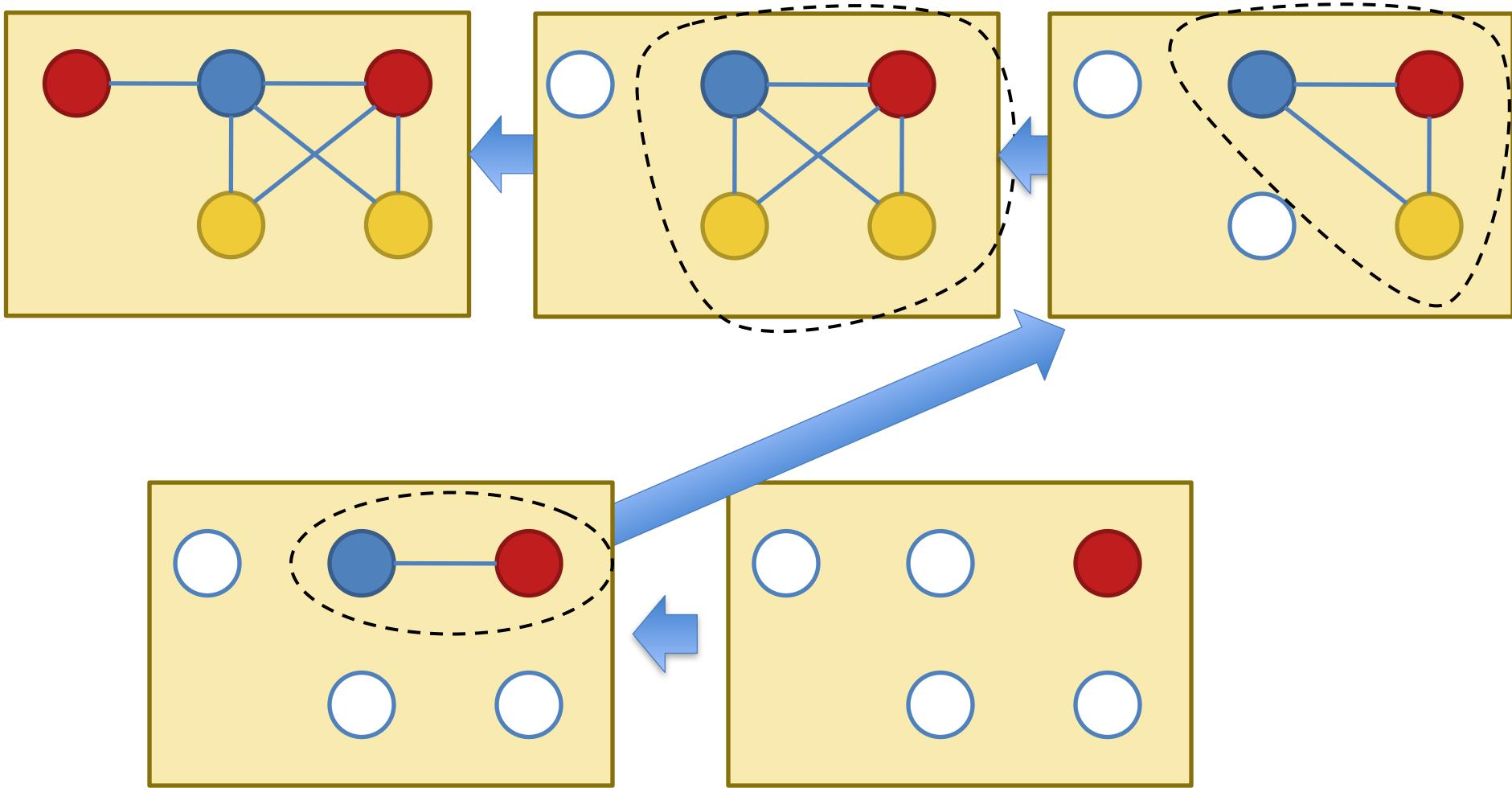
Example: 3-colour this Graph

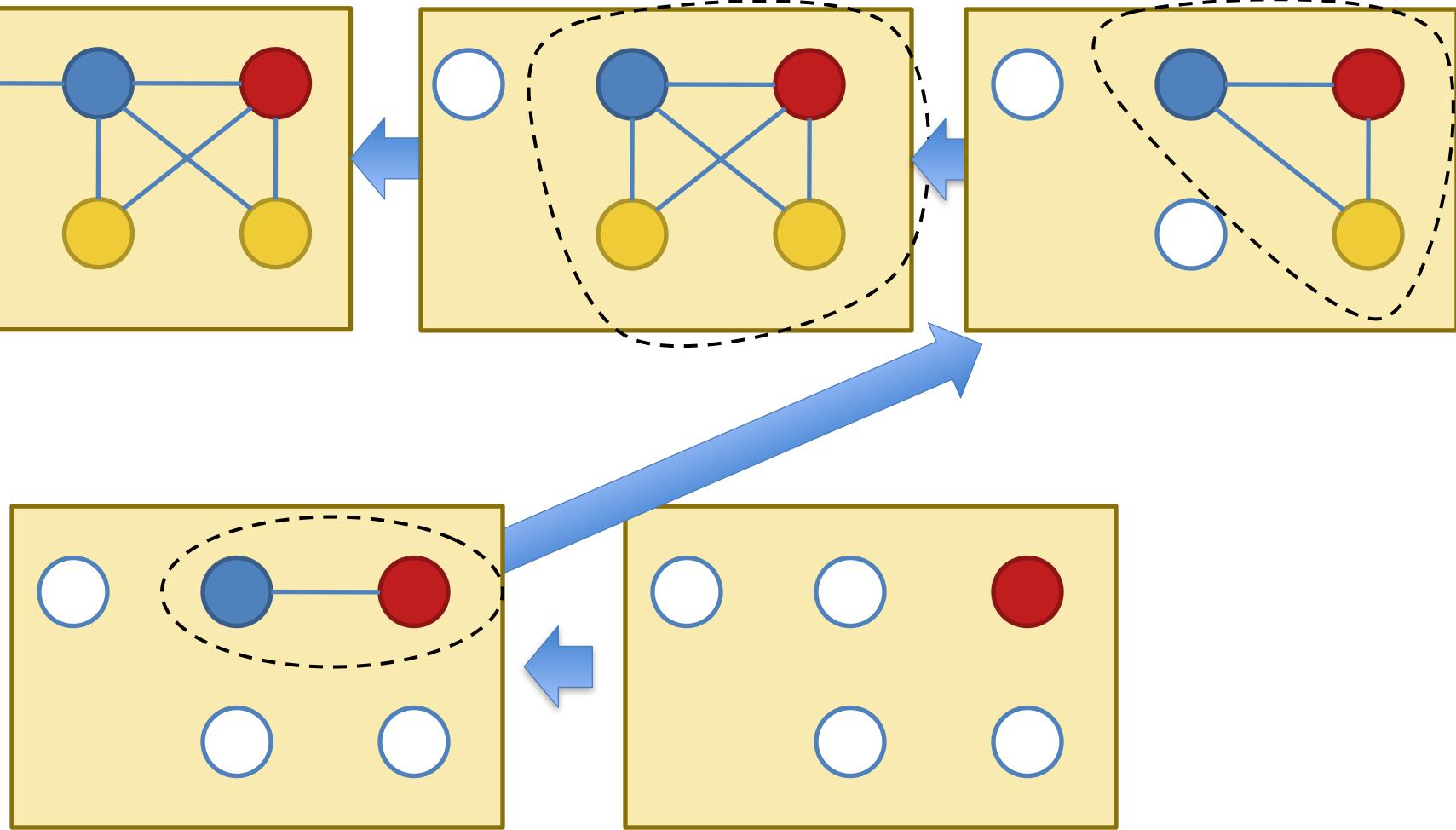




Recursing Down the Simplified Graphs

Example: 3-colour this Graph

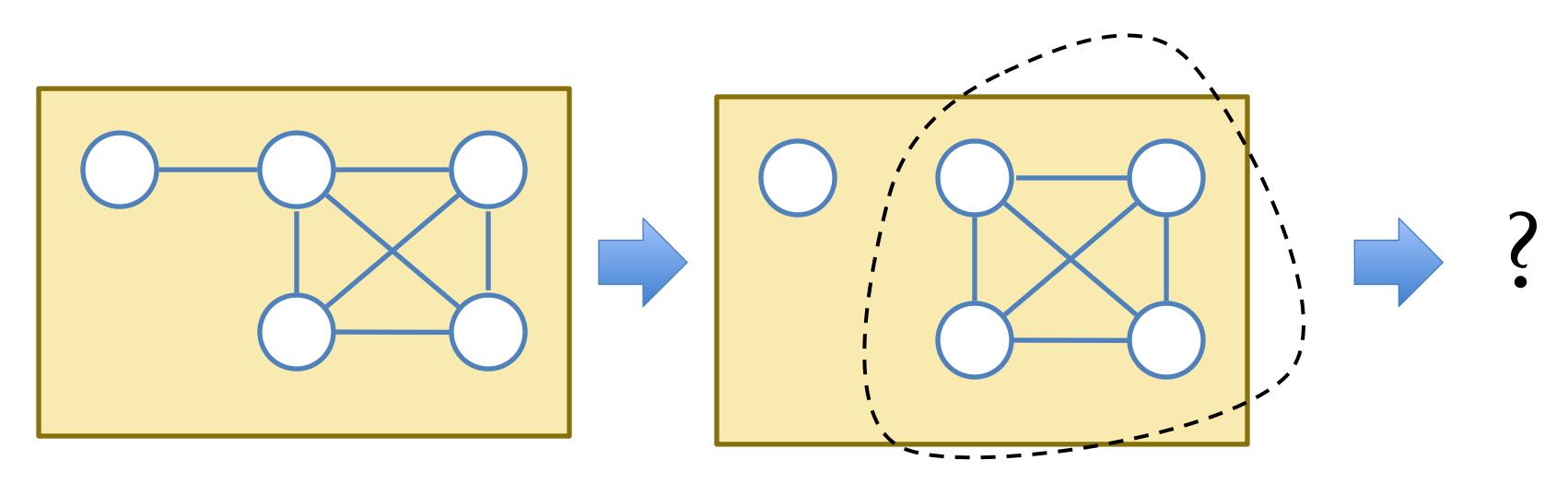




Assigning colours on the way back up.

Failure of the Algorithm

- If the graph cannot be coloured, it will simplify to a graph where every node has at least K neighbours.
 - This can happen even when the graph is K-colourable!
 - This is a symptom of NP-hardness (it requires search)
- Example: When trying to 3-colour this graph:

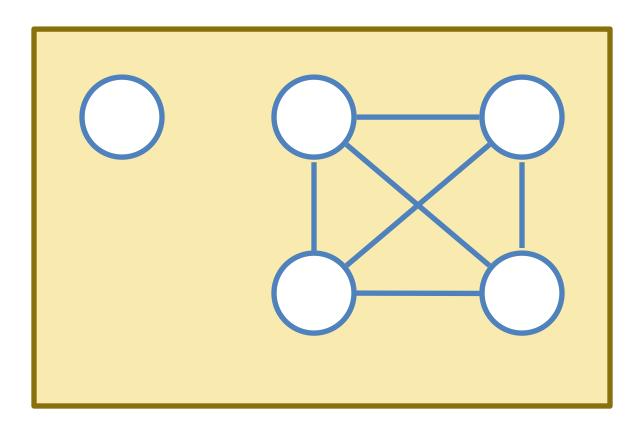


- •
- Which variable to spill? •
 - Pick one that isn't used very frequently
 - Pick one that isn't used in a (deeply nested) loop
 - Pick one that has high interference (since removing it will make the graph easier to colour)
- In practice: some weighted combination of these criteria \bullet
- When colouring: lacksquare
 - Mark the node as spilled
 - Remove it from the graph ____
 - Keep recursively colouring

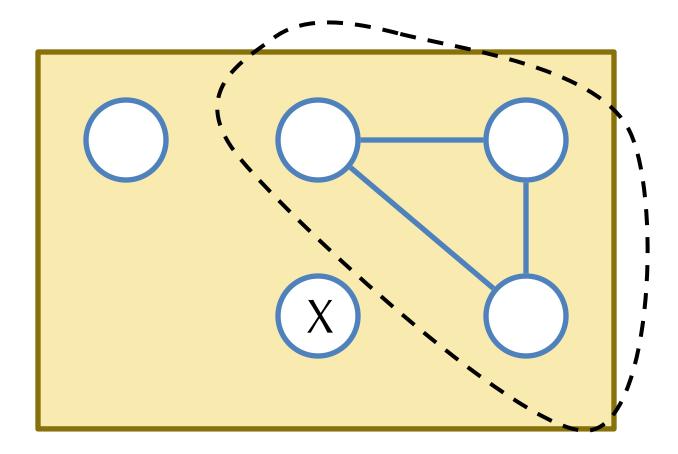


Idea: If we can't K-colour the graph, we need to store one temporary variable on the stack.

- Select a node to spill ullet
- Mark it and remove it from the graph \bullet
- Continue colouring •

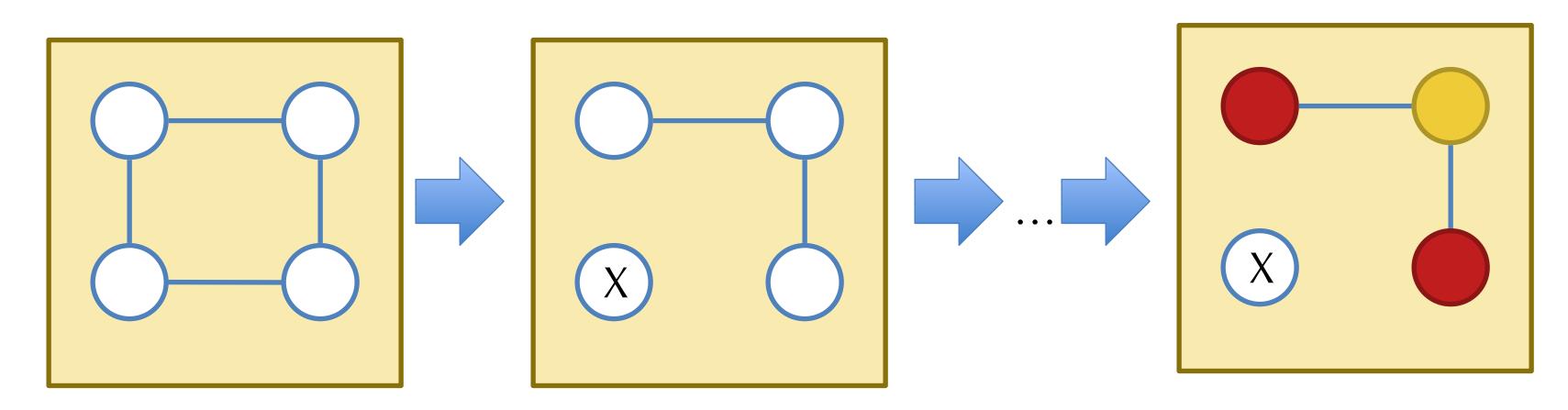






Optimistic Colouring

- Sometimes it is possible to colour a node marked for spilling. ulletIf we get "lucky" with the choices of colours made earlier. —
- Example: When 2-colouring this graph, we don't have a node with degree < 2



- Even though the node was marked for spilling, we can colour it. lacksquare
- So: on the way down, mark for spilling, but don't actually spill...

Pre-coloured Nodes

- Some variables must be pre-assigned to registers.
 - E.g. on X86 the multiplication instruction: IMul must define %rax
 - Arguments of a call have pre-assigned registers
- To properly allocate temporaries, we treat registers as nodes in the interference graph with pre-assigned colours.
 - Pre-coloured nodes can't be removed during simplification.
 - Trick: Treat pre-coloured nodes as having "infinite" degree in the interference graph this guarantees they won't be simplified.
 - When the graph is empty except the pre-coloured nodes, we have reached the point where we start colouring the rest of the nodes.

Picking Good Colours

- lacksquarebut some choices are better for performance.
- Example: \bullet %t1 = %t2
- A simple colour choosing strategy that helps eliminate such moves: \bullet

 - move-related edge.

When choosing colours during the colouring phase, any choice is semantically correct,

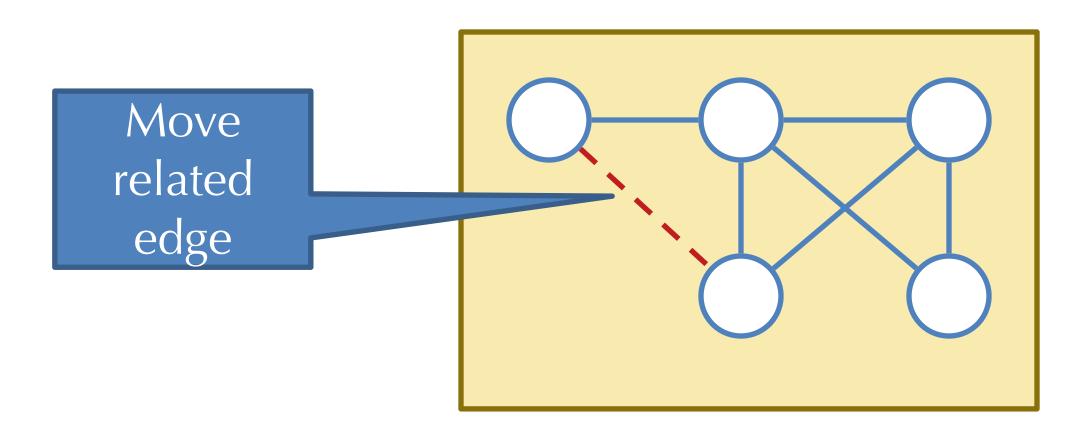
– If t1 and t2 can be assigned the same register (colour) then this move is redundant and can be eliminated.

Add a new kind of "move related" edge between the nodes for t1 and t2 in the interference graph.

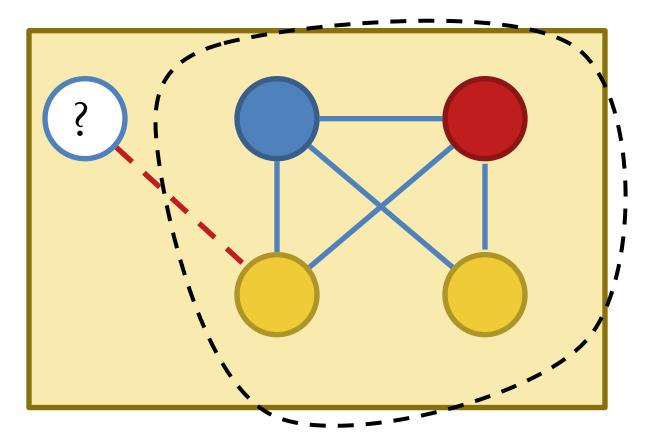
When choosing a colour for t1 (or t2), if possible pick a colour of an already coloured node reachable by a

Example Colour Choice

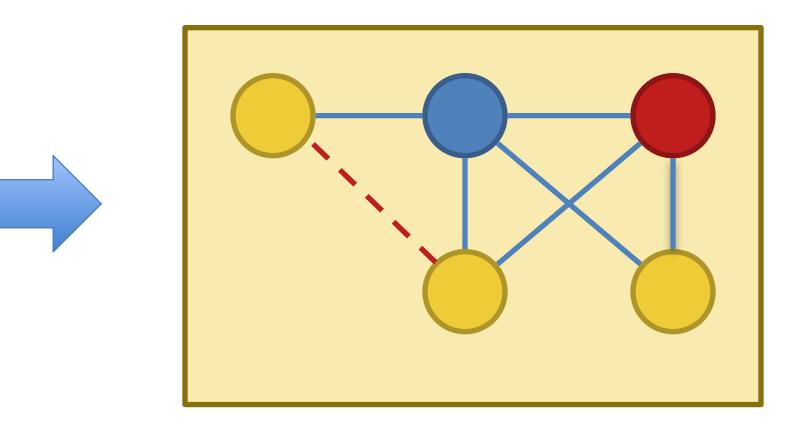
• that there is a Mov from one temporary to another.



- After colouring the rest, we have a choice: \bullet
 - Picking yellow is better than red because it will eliminate a move.

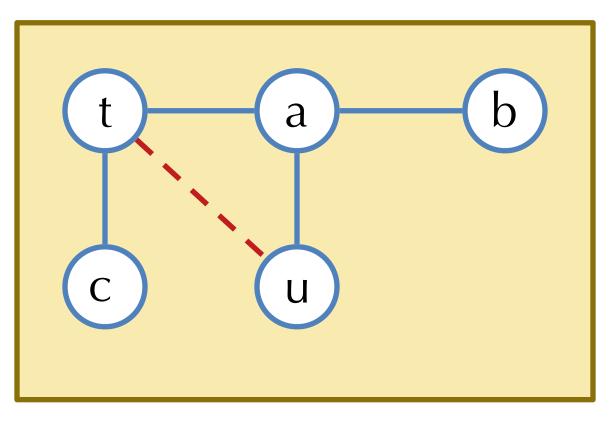


Consider 3-colouring this graph, where the dashed edge indicates

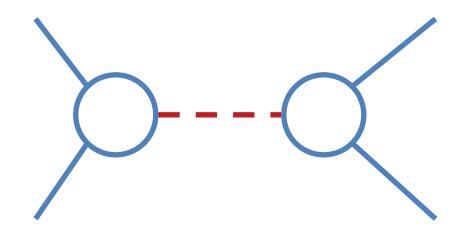


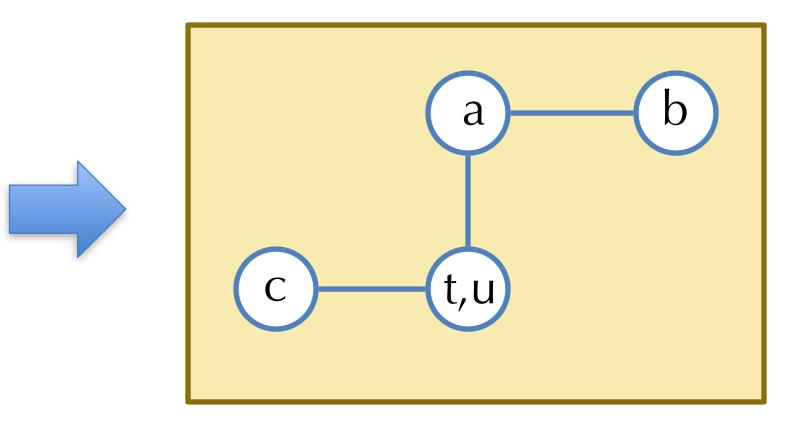
Coalescing Interference Graphs

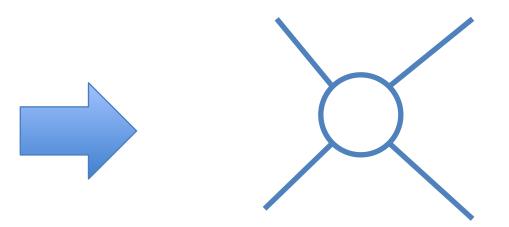
- A more aggressive strategy is to *coalesce* nodes of the interference graph if they are connected by move-related edges.
 - Coalescing the nodes *forces* the two temporaries to be assigned the same register.



- Idea: interleave simplification and coalescing to maximize the number of moves that can be eliminated.
- Problem: coalescing can sometimes increase the degree of a node.







Conservative Coalescing

- Two strategies are guaranteed to preserve the k-colorability of the interference graph.
- Brigg's strategy: It's safe to coalesce **x & y** if the resulting node will have fewer than k neighbours (with degree $\geq k$).
- George's strategy: We can safely coalesce **x** & **y** if for every neighbour **t** of **x**, either **t** already interferes with **y** or t has degree < **k**.

Graph Colouring Algorithm

- Build interference graph (pre-colour nodes as necessary). 1. Add move related edges —
- 2. Reduce the graph (building a stack of nodes to color).
 - a. nodes are high degree or move-related.
 - Coalesce move-related nodes using Brigg's or George's strategy. b.
 - С.
 - If no nodes can be coalesced *freeze* (remove) a move-related edge and keep trying to simplify/coalesce. d.
- 3. step 2.
- 4.
 - а. starting at step 1.

Simplify the graph as much as possible without removing nodes that are move-related (i.e. have a move-related neighbour). Remaining

Coalescing can reveal more nodes that can be simplified, so repeat 2.a and 2.b until no node can be simplified or coalesced.

If there are non-precoloured nodes left, mark one for spilling, remove it from the graph and continue doing

When only pre-coloured node remain, start colouring (popping simplified nodes off the top of the stack). If a node must be spilled, insert spill code as on slide "Example Spill Code" and rerun the whole register allocation algorithm,







Demo: Register allocation in HW6



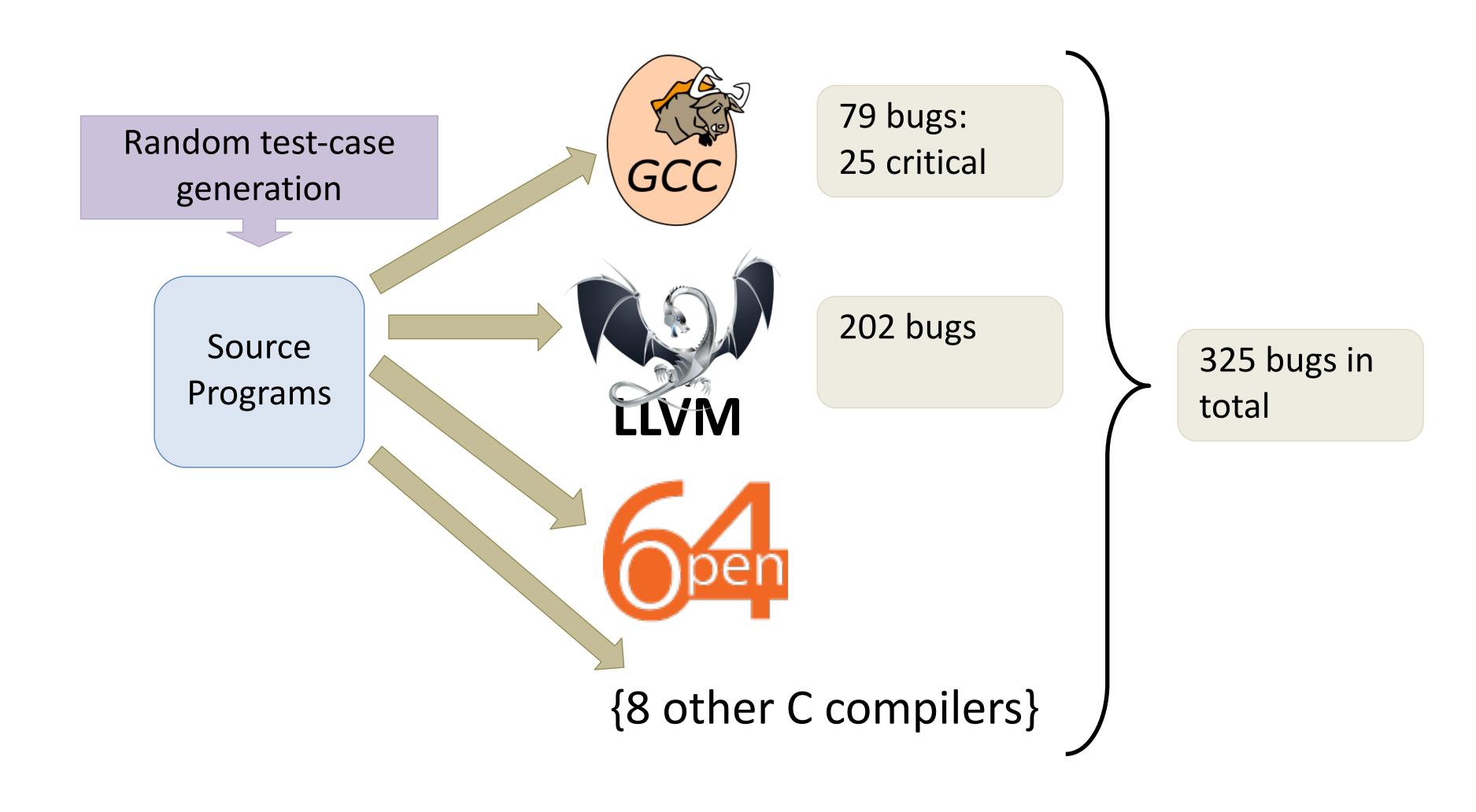
For HW6

- HW 6 implements two naive register allocation strategies:
- no_reg_layout: spill all registers to the stack
- greedy_layout: puts the first few uids in available registers and spills the rest. It uses liveness information to recycle available registers when their current value becomes dead (see the slides above).
- Your job: do "better" than these via graph colouring.
- Quality Metric:
 - the total number of memory accesses in x86 program, which is the sum of:
 - the number of Ind2 and Ind3 operands
 - the number of Push and Pop instructions
 - shorter code is better

Current Research in Programming Languages and Compilers

Validating Compilers

- The job of a compiler is to translate from the syntax of one language to another, but preserve the semantics.
- Compiler correctness is critical
 - Trustworthiness of every component built in a compiled language depends on trustworthiness of the compiler
- Compilers tend to be well-engineered and well-tested, but that does not mean they are *bug-free*.



Testing Compilers

Finding and Understanding Bugs in C Compilers. Yang et al. PLDI 2011



Finding and Understanding Bugs in C Compilers

Yang Chen Eric Eide John Regehr Xuejun Yang University of Utah, School of Computing {jxyang, chenyang, eeide, regehr}@cs.utah.edu

Compilers should be correct.

To improve the quality of C compilers, we created Csmith, a randomized test-case generation tool, and spent three years using it to find compiler bugs.

During this period we reported more than 325 previously unknown bugs to compiler developers.

(in PLDI 2011)

The striking thing about our **CompCert** results is that the middle-end bugs we found in all other compilers are **absent**.

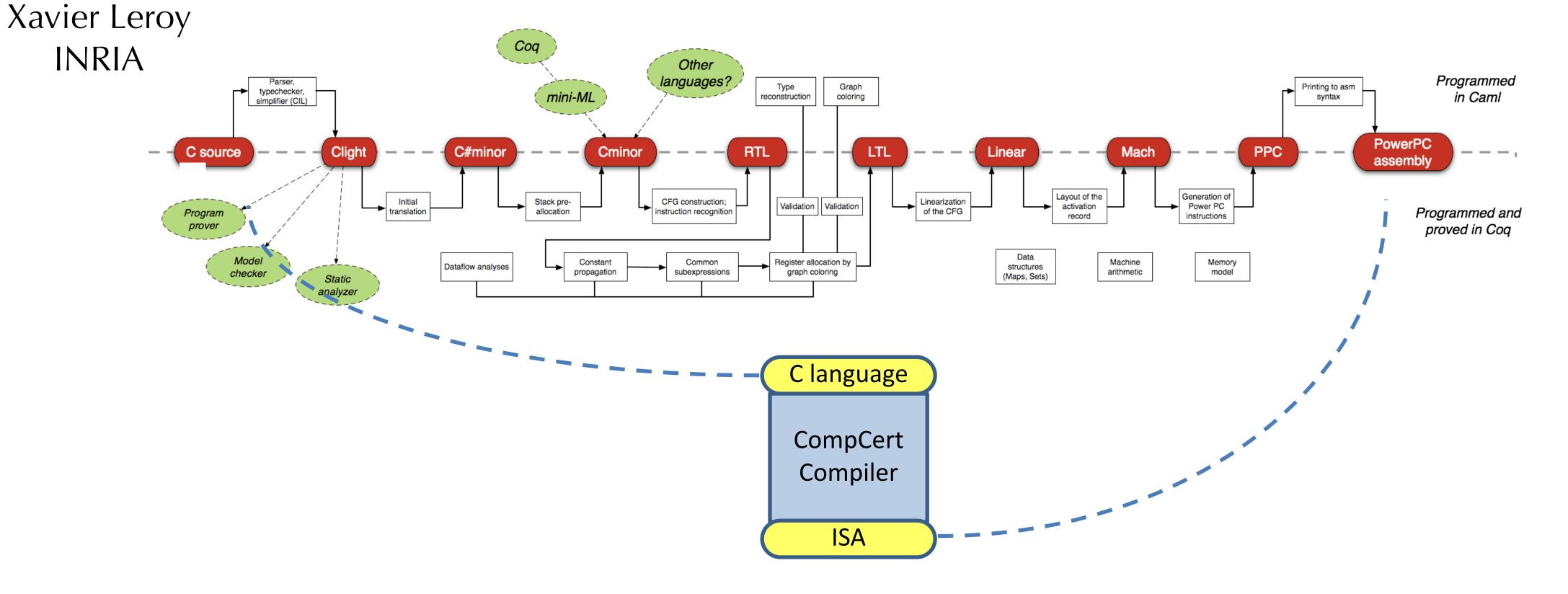
As of early 2011, the under-development version of **CompCert** is the only compiler we have tested for which Csmith cannot find wrong-code errors. This is not for lack of trying: we have devoted about six CPU-years to the task.

The apparent unbreakability of CompCert supports a strong argument that developing compiler optimizations within a proof framework, where safety checks are explicit and machinechecked, has tangible benefits for compiler users.

Verified Compilation

CompCert (2006-now): Optimising C Compiler, proved correct end-to-end





with machine-checked proof in Coq

Comparing Behaviours

• Consider two programs P1 and P2 possibly in different languages. – e.g. P1 is an Oat program, P2 is its compilation to LL

The semantics of the languages associate to each program a set of observable behaviours: •

- Note: $|\mathbf{B}(P)| = 1$ if P is deterministic, > 1 otherwise
- $\mathbf{B}(P1)$ and $\mathbf{B}(P2)$

What is Observable?

• For C-like languages:

• For pure functional languages:

terminates(st) (i.e. observe the final state)

terminates(v) (i.e. observe the final value)

What about I/O?

- Add a *trace* of input-output events performed:
 - t ::= [] | e :: t (finite traces)
 - - observable behavior ::= goeswrong(t)

coind. T := [] | e :: T (finite and infinite traces)

terminates(t, st) (end in state st after trace t) diverges(T) (loop, producing trace T)

 \Rightarrow

 \Rightarrow

- P1: print(1); / st \Rightarrow
- P2: print(1); print(2); / st

• P3: WHILE true DO print(1) END / st

So $\mathbf{B}(P1) \neq \mathbf{B}(P2) \neq \mathbf{B}(P3)$ •

Examples

terminates(out(1)::[],st)

terminates(out(1)::out(2)::[],st)

diverges(out(1)::out(1)::...)

Bisimulation

• Two programs P1 and P2 are *bisimilar* whenever:

$\mathbf{B}(P1) = \mathbf{B}(P2)$

The two programs are completely indistinguishable. •

But... this is often too strong in practice. •

Compilation Reduces Nondeterminism

- Some languages (like C) have underspecified behaviours: - Example: order of evaluation of expressions f() + g()
- Concurrent programs often permit nondeterminism • - Classic optimizations can reduce this nondeterminism
- - Example:

$$a := x + 1; b := x + 1$$

LLVM explicitly allows nondeterminism: • undef values (not part of LLVM lite)

- x := x + 1
- VS.
- a := x + 1; b := a || x := x+1

Backward Simulation

Program P2 can exhibit fewer behaviours than P1: ullet

- All of the behaviours of P2 are permitted by P1, though some of them may have been eliminated. •
- Also called *refinement*. \bullet

 $\mathbf{B}(P1) \supseteq \mathbf{B}(P2)$



Related Research Topics

Automated Parallelisation

- Moore's law: processor advances double speed every 18 months
- Moore's law ended in 2006 for single-threaded applications
- Started to hit fundamental limits in how small transistors can be
- Processor manufacturers shifted to multi-core processors
- Need new compiler technology to take advantage of multi-core automatically find and exploit opportunities for parallel execution

Program Analysis

- The goal of a program analysis is to answer questions about the run-time behaviour of software ullet
- In compilers: data flow analysis, control flow analysis ullet– Typical goal: determine whether an optimisation is safe
- Research in program analysis has shifted to more sophisticated properties: lacksquare
 - *Numerical analyses*, e.g., find geometric regions that contain reachable values for integer variables. Can be used to verify absence of buffer overflows.
 - Shape analyses determine whether a data structure in the heap is a list, a tree, a graph,... Can be used to verify memory safety.
 - *Resource analyses* e.g., find a conservative upper bound on the run-time complexity of a loop. Can be used to find timing side-channel attacks.
 - *Concurrency analysis*: find all data races in a multi-threaded program.
- Industrial program analysis: \bullet
 - Static Driver Verifier (Microsoft): finds bugs in device driver code
 - Infer (Facebook): proves memory safety & finds race conditions

– Astrée (AbsInt): static analyser for safety-critcal embedded code (e.g., automotive& aerospace applications)

Program Verification and Synthesis

- •
- Synthesis: Given a specification, find a program that satisfies the specification •
 - Kind of a "compilation on steroids" from language of specifications to a programming language

Verification: Given a program and a specification, prove that the program satisfies the specification

void swap(loc x, loc y)

{ x ↦ a ∧ y ↦ b }

void swap(loc x, loc y)

 $\{ x \mapsto b \land y \mapsto a \}$

{ x ↦ a ∧ y ↦ b } void swap(loc x, loc y)

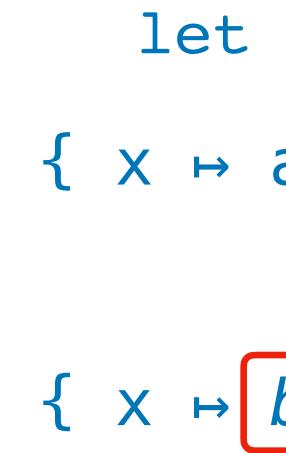
"x and y are different memory locations"

- { x ↦ a ***** y ↦ b }
- void swap(loc x, loc y)
 - $\{ x \mapsto b \not \ast y \mapsto a \}$

{ X ↦ a * Y ↦ b } void swap(loc x, loc y) $\{ X \mapsto b * Y \mapsto a \}$

 $\{ x \mapsto a \ast y \mapsto b \}$ void swap(loc x, loc y) $\{ x \mapsto b \ast y \mapsto a \}$

 $\{ x \mapsto a \ast y \mapsto b \}$?? $\{ x \mapsto b * y \mapsto a \}$



let $a^2 = *x;$ $\{ x \mapsto a2 * y \mapsto b \}$?? { x ↦ b * y ↦ a2 }

- let $a^2 = *x;$
- let b2 = *y;
- { x ↦ a2 * y ↦ b2 }
 - ??
- $\{ x \mapsto b2 * y \mapsto a2 \}$

*x = b2;

- let $a^2 = *x;$
- let b2 = *y;
- $\{ x \mapsto b2 * y \mapsto b2 \}$
 - ??
- $\{ x \mapsto b2 * y \mapsto a2 \}$

*x = b2;*y = a2;

- let $a^2 = *x;$
- let b2 = *y;
- { x ↦ b2 * y ↦ a2 }
 - ??
- $\{ x \mapsto b2 * y \mapsto a2 \}$

*x = b2;*y = a2;

- let $a^2 = *x;$
- let b2 = *y;
- $\{ x \mapsto b2 * y \mapsto a2 \}$
 - ??
- $\{ x \mapsto b2 * y \mapsto a2 \}$

 $x \mapsto b2 * y \mapsto a2 \vdash x \mapsto b2 * y \mapsto a2$

*x = b2;*y = a2; $x \mapsto b2 * y \mapsto a2 \vdash x \mapsto b2 * y \mapsto a2$

- let $a^2 = *x;$
- let b2 = *y;
- $\{ x \mapsto b2 * y \mapsto a2 \}$
 - ??
- $\{ x \mapsto b2 * y \mapsto a2 \}$



*y = a2;

}

- void swap(loc x, loc y) {
 - let $a^2 = *x;$
 - let b2 = *y;
 - *x = b2;

Transforming Entailment

There <u>exists</u> a program **c**, such that for any initial state satisfying P, c, after it terminates, will transform to a state satisfying Q.

$P \rightarrow O$



"'Proof": *x = 42

$EV(\Gamma, P, Q) \cap Vars(R) = \emptyset$ Γ;{P} **→** {Q} | c – (Frame) Γ; { P * R } → { Q * R } | c

F; {emp} → {emp} | skip (Emp)

Γ;

$$a \in GV(\Gamma, P, Q) \qquad \text{y is fresh}$$

$$\Gamma, y; [y/a] \{ \times \mapsto y * P \} \twoheadrightarrow [y/a] \{ Q \} \mid c \qquad (\text{Read})$$

$$\Gamma; \{ \times \mapsto a * P \} \twoheadrightarrow \{ Q \} \mid \text{let } y = *x; c \qquad (\text{Read})$$

$$\Gamma; \{ \times \mapsto e * P \} \rightsquigarrow \{ \times \mapsto e * Q \} \mid c \qquad (\text{Write})$$

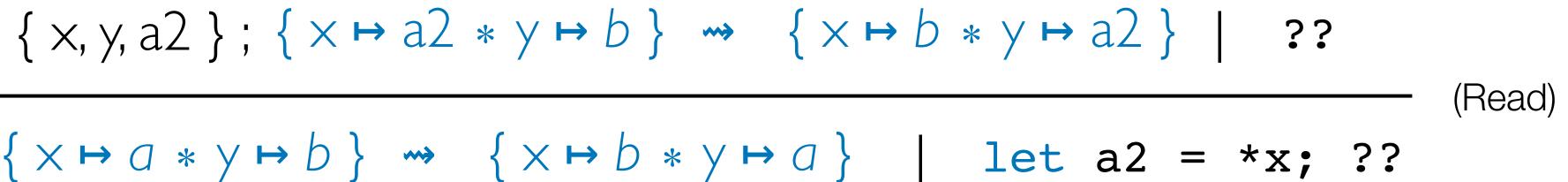
$$\Gamma; \{ \times \mapsto - * P \} \twoheadrightarrow \{ \times \mapsto e * Q \} \mid x = e; c \qquad (\text{Write})$$



- $\{ \times \mapsto a * \gamma \mapsto b \}$
- void swap(loc x, loc y)
 - $\{ \times \mapsto b \ast \gamma \mapsto a \}$



 $\{x, y\}; \{x \mapsto a * y \mapsto b\} \twoheadrightarrow \{x \mapsto b * y \mapsto a\} \mid \text{let a2} = *x; ??$



$\{ x, y, a2, b2 \}; \{ x \mapsto a2 * y \mapsto b2 \}$ $\{ x, y, a2 \}; \{ x \mapsto a2 * y \mapsto b \} \twoheadrightarrow \{ x \mapsto a2 * y \mapsto b \}$

}	~~>	{ ×	⊷ b2	*	y ⊷ a	2 }		??		
⊷ b) *	УÞ	a2 }		let	b2	=	*у;	??	(Read)
⊷ Ł) *	УÞ	a }		let	a2	=	*x;	??	(Read)

 $\{ x, y, a2, b2 \}; \{ x \mapsto b2 * y \mapsto b2$ $\{ x, y, a2, b2 \}; \{ x \mapsto a2 * y \mapsto b2 \} \xrightarrow{\bullet}$ $\{ x, y, a2 \}; \{ x \mapsto a2 * y \mapsto b \} \xrightarrow{\bullet}$ $\{ x, y \}; \{ x \mapsto a * y \mapsto b \} \xrightarrow{\bullet}$ $\{ x, y \}; \{ x \mapsto a * y \mapsto b \} \xrightarrow{\bullet}$

	· (Write)
$\{ x \mapsto b2 * y \mapsto a2 \}$ *x = b2; ??	
$\mapsto b * y \mapsto a2$ let b2 = *y; ??	(Read)
$\{ \mapsto b * \gamma \mapsto a \}$ let a2 = *x; ??	(Read)

{ x, y, a2, b2 }; { y ↦ b2 $\{x, y, a2, b2\}; \{x \mapsto b2 * y \mapsto b2\}$ $\{x, y, a2, b2\}; \{x \mapsto a2 * y \mapsto b2\} \implies$ $\{x, y, a2\}; \{x \mapsto a2 * y \mapsto b\} \Rightarrow \{x \vdash a2 * y \mapsto b\}$ $\{x, y\}; \{x \mapsto a * y \mapsto b\} \twoheadrightarrow \{x\}$

$\{ y \mapsto a2 \} ??$	(Eromo)
	(Frame)
$\{ \times \mapsto b2 * \gamma \mapsto a2 \}$ $*x = b2;$	(Write) ??
$\rightarrow b * y \rightarrow a2$ let b2 = *y;	
$\mapsto b * \gamma \mapsto a$ let a2 = *x;	(Read) ??

{ x, y, a2, b2 }; { y ↦ { x, y, a2, b2 }; { y ↦ b2 $\{x, y, a2, b2\}; \{x \mapsto b2 * y \mapsto b2\}$ $\{x, y, a2, b2\}; \{x \mapsto a2 * y \mapsto b2\}$ $\{x, y, a2\}; \{x \mapsto a2 * y \mapsto b\} \Rightarrow \{x \vdash a2 * y \mapsto b\}$ $\{X, Y\}; \{X \mapsto a * Y \mapsto b\} \twoheadrightarrow \{X\}$

$\rightarrow a2 \} \longrightarrow \{ y \mapsto a2 \} ??$		
	· (Write)	
$\{ y \mapsto a2 \} *y = a2;$??	
	??	(Frame)
$\{ \times \mapsto b2 \ast \gamma \mapsto a2 \} \ast x =$	b2;	(Write) ??
$\mapsto b * y \mapsto a2 \}$ let b2 =	*y; ?	
$\mapsto b * y \mapsto a \}$ let a2 =	*x; ?	(Read)

{ x, y, a2, b2 }; { emp } → { emp } ??	
$\{x, y, a2, b2\}; \{y \mapsto a2\} \twoheadrightarrow \{y \mapsto a2\} ??$	(Frame)
$\{x, y, a2, b2\}; \{y \mapsto b2\} \rightsquigarrow \{y \mapsto a2\} *y = a2$	/
$\{x, y, a2, b2\}; \{x \mapsto b2 * y \mapsto b2\} \twoheadrightarrow \{x \mapsto b2 * y \mapsto a2\}$	
$\{x, y, a2, b2\}; \{x \mapsto a2 * y \mapsto b2\} \twoheadrightarrow \{x \mapsto b2 * y \mapsto a2\} *x$	(Write) = b2; ?? (Read)
$\{x, y, a2\}; \{x \mapsto a2 * y \mapsto b\} \Rightarrow \{x \mapsto b * y \mapsto a2\} $ let b2 =	*y; ??
$\{x, y\}; \{x \mapsto a * y \mapsto b\} \twoheadrightarrow \{x \mapsto b * y \mapsto a\} let a2 =$	(Read)

	{ x, y, a2, b2 };
	{ x, y, a2, b2 } ;
	{ x, y, a2, b2 } ; { y ↦ b2
{ x, y, a2, l	o2}; { × ↦ b2 * y ↦ b2
{ x, y, a2, b2 } ;	$\{ x \mapsto a2 * y \mapsto b2 \} \longrightarrow$
{ x, y, a2 } ; { >	$\langle \mathbf{H} a2 * \mathbf{Y} \mathbf{H} b \} \Rightarrow \{ \mathbf{X} \}$
{ ×, y } ; {	$\times \mapsto a * \gamma \mapsto b \} \twoheadrightarrow \{\times$

$$(Emp)$$

$$(Emp)$$

$$(mp) \leftrightarrow \{emp\} \mid skip$$

$$(Frame) \rightarrow a2 \} \leftrightarrow \{y \mapsto a2 \} \mid ??$$

$$(Write)$$

$$(Write) \rightarrow a2 \} \mid xy = a2; ??$$

$$(Frame) \rightarrow \{x \mapsto b2 \ast y \mapsto a2 \} \mid ??$$

$$(Write) \rightarrow b^{2} \ast y \mapsto a^{2} \mid x = b2; ??$$

$$(Write) \rightarrow b^{2} \ast y \mapsto a^{2} \mid x = b^{2}; ??$$

$$(Read) \rightarrow b^{2} \ast y \mapsto a^{2} \mid 1et b^{2} = *y; ??$$

$$(Read) \rightarrow b^{2} \ast y \mapsto a^{2} \mid 1et a^{2} = *x; ??$$

- void swap(loc x, loc y) {

}

- let $a^2 = *x;$
- let b2 = *y;
- *x = b2;
- *y = a2;

What Can be Synthesised

Data Structure	Id	Description	Proc	Stmt	Code/Spec	Tim
T		swap two	1	4	1.0x	0.2
Integers	2	min of two^1	1	3	$1.1\mathrm{x}$	0.8
	3	length^2	1	6	$1.4\mathrm{x}$	0.4
	4	\max^2	1	11	$1.9 \mathrm{x}$	3.0
	5	\min^2	1	11	$1.9 \mathrm{x}$	2.9
	6	$\operatorname{singleton}^1$	1	4	$0.9 \mathrm{x}$	0.2
	7	deallocate	1	4	$5.5 \mathrm{x}$	0.2
	8	initialize	1	4	$1.6 \mathrm{x}$	0.4
	9	copy^3	1	11	$2.7 \mathrm{x}$	0.6
Cinceles I indeed I int	10	append^3	1	6	$1.1 \mathrm{x}$	0.4
Singly Linked List	11	$delete^3$	1	12	$2.6 \mathrm{x}$	1.2
	12	deallocate two	2	9	$6.2 \mathrm{x}$	0.2
	13	append three	2	14	$2.3 \mathrm{x}$	1.0
	14 r	non-destructive append	2	21	$3.0 \mathrm{x}$	8.0
	15	union	2	23	$5.5 \mathrm{x}$	4.3
	16	$\mathrm{intersection}^4$	3	32	$7.0 \mathrm{x}$	101.
	17	$\mathrm{difference}^4$	2	21	$5.1\mathrm{x}$	4.7
	18	$deduplicate^4$	2	22	$7.3 \mathrm{x}$	1.8
	19	$prepend^2$	1	4	$0.4 \mathrm{x}$	0.2
	20	insert^2	1	19	$3.1\mathrm{x}$	1.0
Contod list	21	insertion sort^2	1	7	$1.2 \mathrm{x}$	0.7
Sorted list	22	sort^4	2	13	$4.9\mathrm{x}$	1.0
	23	$\mathrm{reverse}^4$	2	11	$4.0 \mathrm{x}$	0.7
	24	merge^2	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	4.4x	55.6	
	25	$singleton^1$	1	5	1.1x	0.2
	26	copy	1	22	4.3x	7.2
Doubly Linked List	27	$append^3$	1	10	1.6x	1.7
	28	$delete^3$	1	19	3.7x	3.4
	29	single to double	1	23	$6.0 \mathrm{x}$	0.7

What Can be Synthesised

Data Structure	Id	Description	Proc	Stmt	Code/Spec	Time
	25	$singleton^1$	1	5	1.1x	0.2
	26	copy	1	22	$4.3 \mathrm{x}$	7.2
Doubly Linked List	27	append^3	1	10	$1.6 \mathrm{x}$	1.7
	28	$delete^3$	1	19	$3.7 \mathrm{x}$	3.4
	29	single to double	1	23	$6.0 \mathrm{x}$	0.7
	30	deallocate	2	11	10.7x	0.2
List of Lists	31	$flatten^4$	2	17	$4.4 \mathrm{x}$	0.6
	32	length^5	2	21	$5.5 \mathrm{x}$	22.8
	33	size	1	9	$2.5 \mathrm{x}$	0.4
	34	deallocate	1	6	$8.0 \mathrm{x}$	0.2
	35	deallocate two	1	16	11.8x	0.4
	36	copy	1	16	$3.8 \mathrm{x}$	2.5
Binary Tree	37	flatten w/append	1	17	$4.8 \mathrm{x}$	0.4
	38	flatten w/acc	1	12	$2.1\mathrm{x}$	0.6
	39	flatten	2	23	$7.1\mathrm{x}$	1.5
	40	flatten to dll in place	2	15	$9.6 \mathrm{x}$	11.3
	41	flatten to dll w/null ⁵	2	17	11.2x	106.1
	42	insert^2	1	19	2.8x	14.6
	43	rotate $left^2$	1	5	$0.2 \mathrm{x}$	6.2
	44	rotate $right^2$	1	5	$0.2 \mathrm{x}$	4.9
DCT	45	find \min^5	1	11	$1.4\mathrm{x}$	66.3
BST	46	find \max^5	1	18	$2.2 \mathrm{x}$	58.0
	47	delete $root^2$	1	18	1.3x	13.9
	48	from $list^4$	2	27	$5.7 \mathrm{x}$	10.0
	49	to sorted $list^4$	rotate left21rotate right21find min51find max51delete root21from list42to sorted list43		$7.7 \mathrm{x}$	20.8
	50	deallocate	2	9	12.0x	0.2
Rose Tree	51	flatten	3	25	8.0x	11.0
	52	copy^5	2	32	$7.9 \mathrm{x}$	_
Decled Trees	53	pack^5	1	16	1.6x	_
Packed Tree	54	unpack^5	1	23	$2.9 \mathrm{x}$	21.0

More Program Synthesis

B	5 •∂•∓					Roster - Excel			⊞ –
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1	Name	First	Last						
2	Ned Lanning	Ned						bati	terns
3	Margo Hendrix	Margo							
4	Dianne Pugh	Dianne							
5	Earlene McCarty	Earlene							and
6	Jon Voigt	Jon							and
7	Mia Arnold	Mia							
8	Jorge Fellows	Jorge						sha	ows a
9	Rose Winters	Rose							
10	Carmela Hahn	Carmela							
11	Denis Horning	Denis						D re	view
12	Johnathan Swope	Johnathar							
13	Delia Cochran	Delia							
14	Marguerite Cervantes	Marguerit							
15	Liliana English	Liliana							
16	Wendy Stephenson	Wendy							

Excel[®] FlashFill



Wrapping Up



- We have learned (hopefully):
 - How high-level languages are implemented in machine language
 - (A subset of) Intel x86 architecture
 - (A subset of) LLVM
 - Lexing and parsing
 - Lambda-calculus and its extensions
 - A little about programming language semantics and type systems
 - How to implement a type checker
 - How to implement a program analyser
 - How to implement a program optimiser
 - Practical applications of theory (logic, proofs, automata, graphs, lattices)
 - How to represent complex data structures in memory
 - How to write large working programs in OCaml
 - How to be a better programmer

Why CS4212?

Where else is this stuff applicable?

- Understanding hardware/software interface \bullet
 - Different devices have different instruction sets, programming models
- General programming
 - In C/C++, better understanding of how the compiler works can help you generate better code. – Ability to read assembly/LLVM output from compiler

 - Experience with functional programming gives you different ways to think about solving a problem Knowledge of type systems helps you understand type errors in Java, Scala, OCaml, etc.
- Writing domain specific languages
 - lex/yacc very useful for little utilities
 - understanding abstract syntax specification
 - understanding typing rules
 - being able to write *your own* interpreter and compiler

- We skipped stuff at every level... ullet
- Concrete syntax/parsing:
 - Much more to the theory of parsing... LR(*)
 - Good syntax is art not science!
- Source language features:
- Intermediate languages: •
- Compilation: •
 - Continuation-passing transformation, analyses for SSA, compiling OO classes, lambda-lifting, closure conversion
- Analysis and Optimisations: •
 - Abstract interpretation, cache optimization, instruction selection/optimization
- Runtime support:
 - memory management, garbage collection

Stuff we didn't cover

– Exceptions, advanced type systems, type inference, dependent types, concurrency

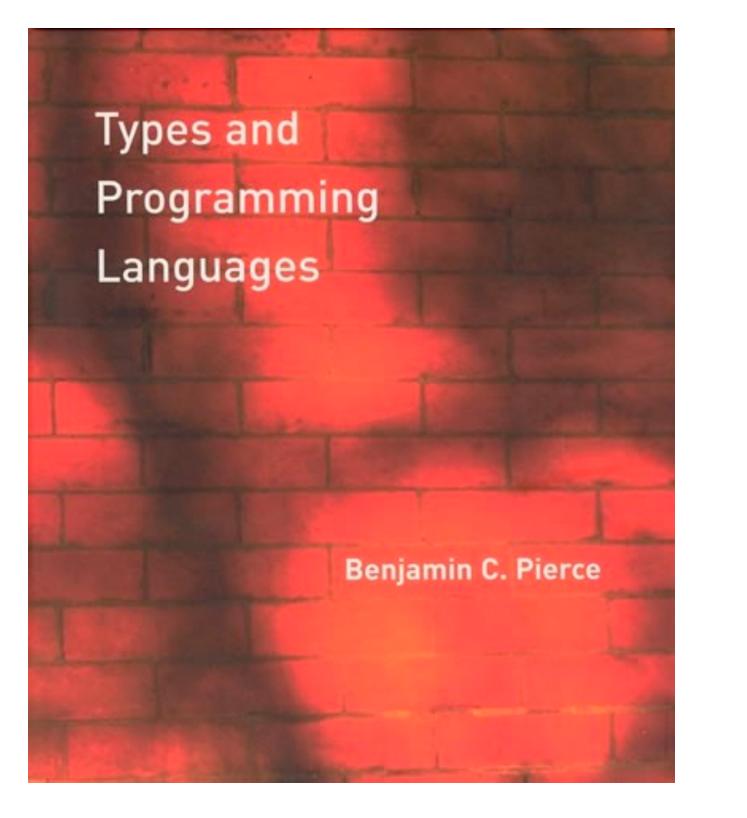
– Intermediate language design, bytecode, bytecode interpreters, just-in-time compilation (JIT)

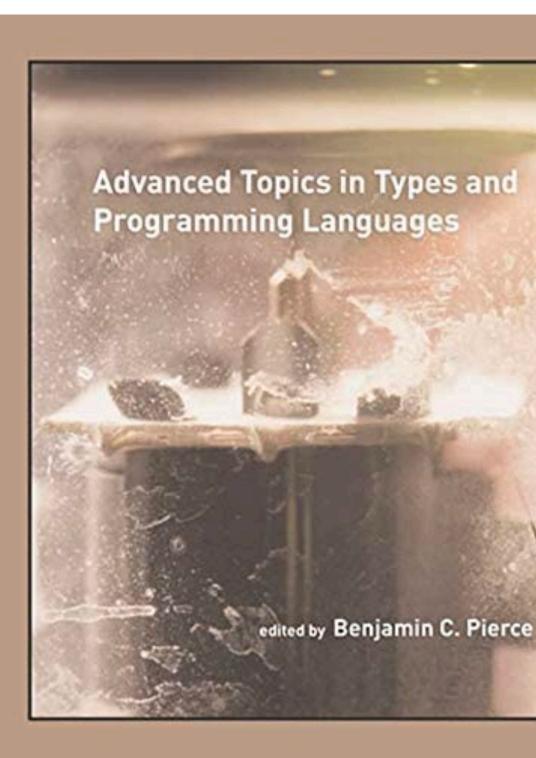
Where to go from here?

- Conferences (proceedings available on the web):
 - Programming Language Design and Implementation (PLDI)
 - Principles of Programming Languages (POPL)
 - Object Oriented Programming Systems, Languages & Applications (OOPSLA)
 - International Conference on Functional Programming (ICFP) ____
- Programming Language Mentoring Workshops (PLMW) Affiliated with POPL/PLDI/OOPSLA/ICFP
- Technologies / Open Source Projects
 - Yacc, lex, bison, flex, ...
 - LLVM low level virtual machine
 - ____
 - Languages: OCaml, F#, Haskell, Scala, Go, Rust, ... Coq, Agda, ...?

Java virtual machine (JVM), Microsoft's Common Language Runtime (CLR)

Further Reading - Types





SOFTWARE FOUNDATIONS VOLUME 1

Logical Foundations

Benjamin Arthur Azo Chris Casi Marco Ga Michael G Cătălin Hr Vilhelm Sj Brent Yorş SOFTWARE FOUNDATIONS VOLUME 2

Programming Language Foundations

Version 6.1 (202

Benjamin C. Pierce Arthur Azevedo de Amorim Chris Casinghino Marco Gaboardi Michael Greenberg Cătălin Hriţcu Vilhelm Sjöberg Andrew Tolmach Brent Yorgey

with

Loris D'Antoni, Andrew W. Appel, Arthur Chargueraud, Michael Clarkson, Anthony Cowley, Jeffrey Foster, Dmitri Garbuzov, Michael Hicks, Ranjit Jhala, Ori Lahav, Greg Morrisett, Jennifer Paykin, Mukund Raghothaman, Chung-Chieh Shan, Leonid Spesivtsev, Philip Wadler, Stephanie Weirich, Li-Yao Xia, and Steve Zdancewic

https://softwarefoundations.cis.upenn.edu/

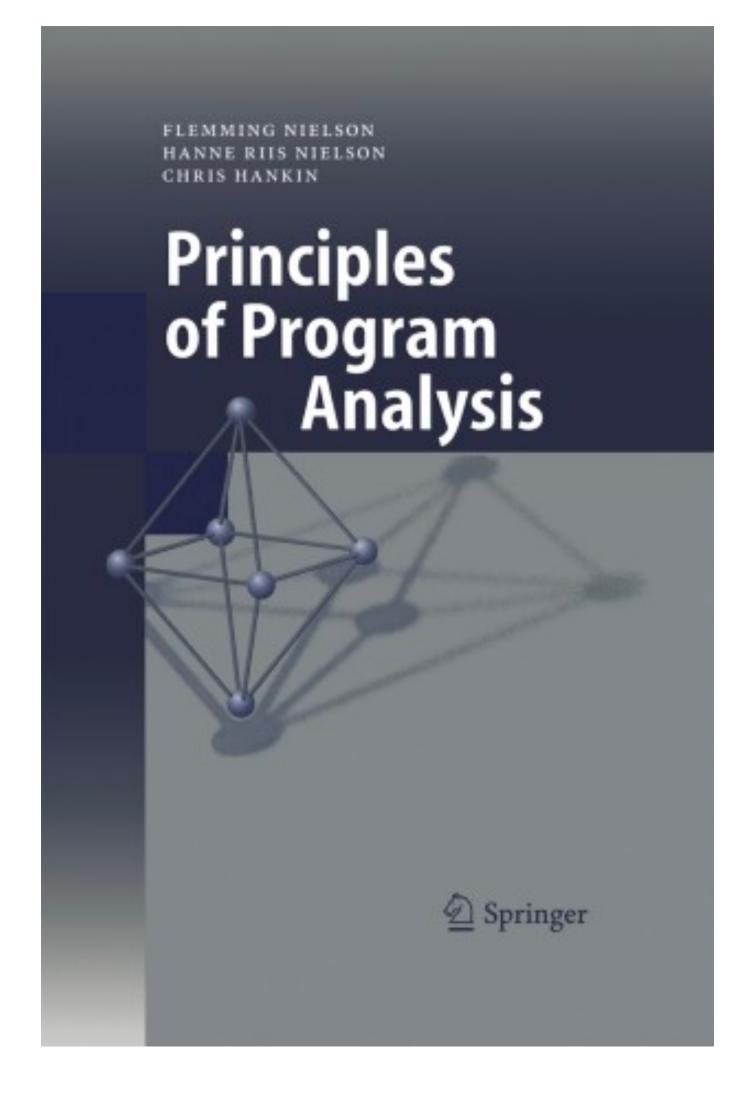
Version 6.1 (2021-08-11 15:14, Coq 8.12 or later)



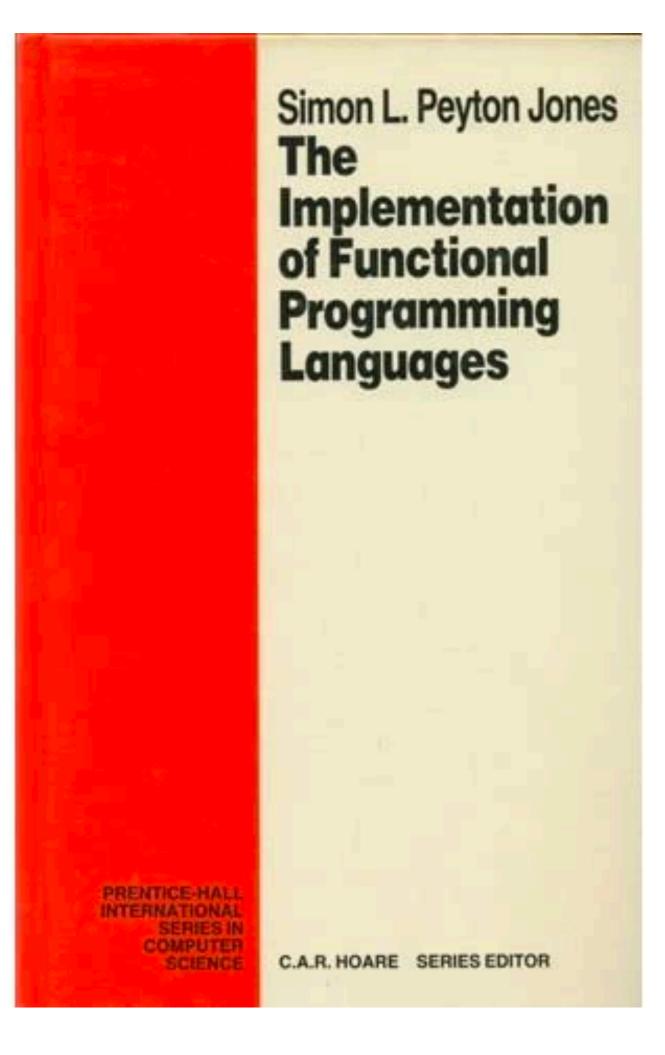
INTRODUCTION TO STATIC ANALYSIS

AN ABSTRACT INTERPRETATION PERSPECTIVE XAVIER RIVAL AND KWANGKEUN YI





Further Reading - Compilation Techniques



Compiling with Continuations Andrew W. Appel

PL Classes at NUS School of Computing

- CS4215: Programming Language Implementation
 - semantics, type systems, automatic memory management, dynamic linking and just-in-time compilation, as features of modern execution systems
- CS5218: Principles and Practice of Program Analysis • foundations of static program analysis, abstract interpretation, lattice theory,
 - analysis of higher-order languages
- CS6217: Topics in Programming Languages & Software Engineering different topics every year, this year: deductive program verification •

 - see <u>https://ilyasergey.net/CS6217/</u>

PL & Compiler Research @ NUS SoC

nus-plse.github.io

or google "NUS PLSE"



The End



